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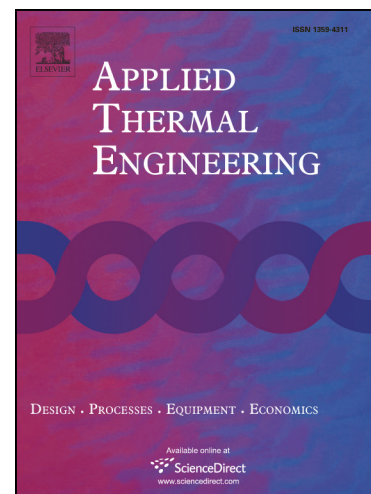
### Experimental and Numerical Investigations of Thermal Characteristics of Heat Exchangers in Oscillatory Flow

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**Experimental and Numerical Investigations of Thermal Characteristics of Heat  
Exchangers in Oscillatory Flow**

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## Abstract

Heat exchangers under oscillatory flow conditions constitute a critical component of thermoacoustic engines and coolers for which effective design methodologies are not yet available. In this study, the thermal and pressure drop performance of compact Tube Heat Exchanger (T-HEX) under oscillatory flow conditions is investigated using experimental and numerical methods. A standing wave experimental set-up, driven by the Q-drive linear alternator, and a measurement technique were developed to measure the temperature and acoustic pressure near the T-HEX simultaneously. The symmetric arrangement of three identical heat exchangers, one 'hot' heat exchanger, centrally placed between two 'cold' heat exchangers, is employed for an improved thermal analysis. Furthermore, aerodynamic shape is used on the heat exchangers gas channels to improve flow conditions associated with a sudden change in the cross-section. Experimental results are found to agree well with the predictions from three-dimensional Computational Fluid Dynamics (CFD) models. The Nusselt number and pressure drop due to minor losses show dependency on the drive ratio (measured maximum oscillating pressure to the system mean pressure), the edge shape and hot heat exchanger temperature. At a high amplitude, the edge shape significantly minimises the minor loss pressure difference, with negligible effect on the thermal performance. The results reported in this study will benefit the development of compact heat exchangers for the thermoacoustic engines/refrigerators or Sterling engines/coolers in cryogenic applications.

## Keywords

Heat exchanger, Heat transfer, Oscillatory flow, Thermoacoustics

## Nomenclature

$A$	Cross sectional area, $\text{m}^2$
$a$	Speed of sound, $\text{m/s}$
$c_p$	Specific heat capacity, $\text{J/kg}\cdot\text{K}$
$DR$	Drive ratio ( $p_o/p_m$ )
$f$	Frequency, $\text{Hz}$
$f_c$	Frontal core diameter, $\text{m}$
$h$	Heat transfer coefficient
$K$	Minor loss coefficient
$k$	Thermal conductivity, $\text{W/m}\cdot\text{K}$
$k'$	Wave number, $\text{rad/m}$
$N$	Sample number
$Nu$	Nusselt number ( $Nu = hD_h/k$ )
$P$	Pressure, $\text{Pa}$
$p$	Oscillating pressure, $\text{Pa}$
$Pr$	Prandtl number ( $Pr = \mu c_p/k$ )
$\dot{Q}$	Heat transfer rate, $\text{W}$
$q$	Heat flux, $\text{W/m}^2$
$R$	Gas constant, $\text{J/kg}\cdot\text{K}$
$SS$	Stainless steel
$Re$	Reynolds number, ( $Re = \rho u D_h/\mu$ )
$r$	Radius, $\text{m}$
$d_h$	Hydraulic diameter, $\text{m}$
$d_t$	Tube diameter, $\text{m}$
$T$	Temperature, $\text{K}$ , $^\circ\text{C}$
$t$	Time, $\text{s}$

$u$	Acoustic velocity in $x$ direction, m/s
$\mathbf{v}$	Velocity vector, m/s
$x$	Distance in $x$ -direction (axial location), m

**Greek letters**

$\Delta$	Difference
	Distance, m
$\delta_k$	Thermal penetration depth, m
$\delta_v$	Viscous penetration depth, m
$\lambda$	Wavelength, m
$\mu$	Dynamic viscosity, kg/m·s
$\xi$	Gas displacement amplitude, m
$\pi$	3.14159
$\rho$	Density, kg/m <sup>3</sup>
$\sigma$	Porosity
$\sigma'$	Viscous stress tensor, Pa
$\phi$	Phase angle, degree (°)
$\varphi$	Scalar variable
$\varphi'$	Fluctuating component of scalar variable
$\omega$	Angular frequency, rad/s

**Subscripts**

$C, c$	Cold
$c1, c2$	Cold heat exchangers 1 and 2
$fr$	Frontal
$g$	Gas
$H, h$	Hot
$hx$	Heat exchanger

<i>i, in, inlet</i>	Inlet
<i>ins</i>	Insulation
<i>loss</i>	Loss
<i>m</i>	Mean value
<i>out, outlet</i>	Outlet
<i>s</i>	Surface
<i>v</i>	volume
<i>w</i>	Water
<i>0</i>	Reference condition
<i>1</i>	First order of acoustic variable, Count

#### Special symbols

$\nabla$	Spatial gradient, difference
$\partial$	Partial derivative
Overbar	Time average

#### Abbreviation

<i>CAD</i>	Computer Aided Design
<i>CFD</i>	Computational Fluid Dynamics
<i>CHX</i>	Cold Heat exchanger
<i>HHX</i>	Hot Heat exchanger
<i>LDS</i>	Laser Displacement Sensor
<i>PISO</i>	Pressure-Implicit with Splitting of Operators
<i>PIV</i>	Particle Image Velocimetry
<i>PLIF</i>	Planar Laser-Induced Fluorescence
<i>RANS</i>	Reynolds-averaged Navier-Stokes
<i>RC</i>	Curvature Radius
<i>RMSRe</i>	Root Mean Square Reynolds number
<i>SST</i>	Shear Stress Transport
<i>TASFE</i>	Time Averaged Steady Flow Equivalent
<i>T-HEX</i>	Tube Heat Exchanger

*UDF*

User-Defined Function

ACCEPTED MANUSCRIPT

## 1.0 Introduction

For the development of thermoacoustic engines and coolers with high performance, an optimum design for the heat exchanger is an essential requirement. A typical thermoacoustic system employs oscillatory flow as a means of energy transfer within its internal elements (heat exchangers, stack or regenerator) to produce acoustic power (engine) or consume it for heat pumping (cooler). Either in thermoacoustic engine or cooler, heat exchangers act as a heat source and heat sink, which implies that the efficiency of the device can be improved through an optimised heat exchanger design. A detailed description of the fundamental of energy transfer and the Sterling-like thermoacoustic cycle that is responsible for thermoacoustic effect in the heat exchange components of thermoacoustic systems has been described by Swift (1998, 2002).

The two primary design considerations for a heat exchanger in oscillatory flow are to maximise heat transfer for relatively short acoustic displacement of the oscillating gas and to minimise pressure losses. Both considerations depend on flow conditions and suggest that the geometric design of a heat exchanger can affect its thermal and minor loss pressure drop performance. Unlike the heat exchangers in steady flow which has well-established design guidelines, the presence of acoustically induced flow and the cyclic flow reversal at certain distances in energy system such as thermoacoustic devices, implies that the heat transfer cannot arbitrarily be increased by increasing the heat transfer area of the heat exchanger. This makes the design and optimisation of heat exchangers in oscillatory flow a challenging task, which forms the basis for the lack of effective oscillatory flow design methodologies.

In the design of heat exchangers in oscillatory flow, the commonly used methods include the quasi-steady approximations such as the well-known TASFE (Time-Average Steady-Flow Equivalent) (Richardson, 1967) and RMSRe (Root Mean Square Reynolds Number), which



are based on heat transfer correlation from steady flow conditions. However, it has been reported (Mozurkewich, 2001; Piccolo and Pistone, 2006) that these approximations did not hold at higher oscillating velocities which result in overprediction of heat transfer as well as underprediction of the minor losses (Morris et al., 2004). Also, the heat transfer model based on boundary layer conduction over predicts heat transfer in oscillatory flow (Paek et al., 2005). Therefore, the design and development of heat exchangers in oscillatory flow would require further study to achieve a more reliable performance data for establishing detailed design guidelines.

Research works have been carried out to study the thermal performance of heat exchangers in oscillatory flow. Finned type heat exchangers (Nsofor et al., 2007; Tang et al., 2013, 2014; Kamsanam et al., 2015), parallel plate type (Wakeland and Keolian, 2004; Shi et al. 2010), and parallel tube types (Mozurkewich, 2001) have been studied to determine the influence of normalised displacement amplitude, fin or plate spacing, plate thickness, and acoustic Reynolds number (based on the peak acoustic velocity between tubes), on the heat transfer performance of heat exchangers. These studies have used either a single ambient or cold heat exchanger for heat transfer performance characterisation or a pair of adjacent ‘cold’ and ‘hot’ heat exchangers (with or without gap) in an attempt to improve the heat transfer estimation and to propose oscillatory flow correlations. However, the issue of heat leak through the working fluid to the surrounding could not be resolved entirely because of lack of symmetry in the heat exchanger arrangement. This suggests that the heat transfer estimation in oscillatory flow can still be improved by using a symmetric arrangement of heat exchangers, to arrive at a more accurate design guidelines for the oscillatory flow heat exchangers.

The edge shape of a heat exchanger is of high importance in thermoacoustics and can be explored for an optimum design that is capable of minimising the minor losses associated with a change in cross-section of the gas channels, which often translate into a nonlinear

acoustic impedance that can diminish the efficiency of the system (Petculescu and Wilen, 2002; Olson and Swift, 1997), thereby contributing to the overall system efficiency. It is interesting to know that the studies above considered heat transfer and fluid flow conditions through square-edged geometries, which often produce disturbances that may generate minor losses and impact pressure drop performance negatively. In thermoacoustic engines and coolers, heat exchangers are placed near to the stack/regenerator with a small separation gap, and it would appear reasonable that this arrangement may alter the nonlinear impedances of the heat exchangers by reducing jetting and vortex formation and shedding. On the other hand, if the flow is modified, for example by using aerodynamic edge shape, in such a way to mitigate these non-linear effects, there may be a corresponding effect on the heat transfer. The works of Smith and Swift (2002), Marx et al. (2004) focused on the experimental investigation of the effect of rounded edge on flow ducts against parametric operating conditions, but no heat exchanger was investigated and it unclear what the effect of edge shape will be on the heat transfer and pressure drop performance. Therefore, the extent of geometric effect on the performance of a heat exchanger in oscillatory flow needs to be considered, and it is one of the objectives of this paper.

Another important area in the study of heat transfer in oscillatory flow is the determination of heat transfer coefficient on the gas side of the heat exchanger. In oscillatory flow, the fluid temperature changes in time and location due to the forward and backward movement of the gas particles, which in turn dictate different heat transfer behaviour to that of steady flow. Currently, there appears to be no consensus in the literature over the definition of the heat transfer coefficients in the oscillatory flow, which has been defined to be application dependent in the relevant research studies (Zhao and Cheng, 1995; Brewster et al., 1997; Shi et al., 2010).

To understand the heat transfer phenomenon in oscillatory, it may be worthwhile to investigate the fundamental features of the velocity and temperature fields that show the flow behaviour and how it affects the heat transfer performance of the heat exchangers. Several methods have been used for this purpose including the Particle Image Velocimetry (PIV) (Aben et al., 2009) and Planar Laser Induced Fluorescence (PLIF) (Shi et al., 2010), numerical simulations (Worlikar and Knio, 1999; Mohd Saat, 2013) and combination of techniques (Yu et al., 2014). These methods provide useful information, in two-dimension, for the understanding of flow physics in a parallel plate structure under oscillatory flow. However, the information about the three-dimensional (3D) effects (Swift, 2002) which are present for the compact heat exchangers still requires further investigation. A 3D CFD model offers the advantage of providing useful information that can complement the experimental data to give an understanding of the heat transfer and flow physics inside the heat exchangers in oscillatory flow. In the CFD technique to modelling of thermoacoustic engines and refrigerators (Nijeholt et al., 2005; Zink et al., 2010a and 2010b), the internal elements are often accounted for by using porous media method, where a volume porosity is used to account for the solid fraction, and the pressure loss of the heat exchanger is evaluated using the steady flow relation (Kays and London, 1964; Thomas and Pittman, 2000). While this approach reduces the computational effort for modelling the whole thermoacoustic device, it does not give information about the contribution of each constituent element of the system such as the thermal interaction of working fluid with the thermal contact area of the heat exchangers. Therefore, modelling the actual configuration of the heat exchanger will provide more interesting information on nonlinear phenomena like turbulence, streaming and vortex shedding, which is required for the design needs, but cannot be captured with the existing classic linear theory or the simplified geometries.

This paper focuses on the investigation of the heat transfer, and pressure drop due to minor losses in the Tube-Heat Exchangers (T-HEX) under oscillatory flow, using experimental and numerical methods. In the experimental aspect, a purpose-built setup and measurement techniques are specifically developed to test the heat exchangers (without a stack or regenerator) under high pressure and oscillatory flow conditions as relevant to thermoacoustic systems. In the numerical aspect, 3D CFD models are developed and validated based on the same geometric dimensions of the T-HEX and the measurement data in the experiments. Comparison between experimental and simulation results are first carried out. Further analyses are then performed with the simulation results to extend the understanding of the thermal-fluid processes in oscillatory flow. The investigations are carried out by examining the effect of geometry (edge shape), drive ratio (measured maximum oscillating pressure and the system's mean pressure) and temperature of the hot heat exchanger. These effects are considered in the pressure amplitude distribution, averaged temperature, velocity amplitude and flow structure, heat fluxes, Nusselt number, and the pressure drop due to minor losses.

The significance of this study includes the use of a symmetric arrangement of heat exchangers to improve the heat transfer estimation on a T-HEX. Also, an aerodynamic edge-shape is used on the T-HEX (ogive) gas channel, to modify the flow condition and minimise the pressure drop due to minor losses, with negligible effect on the heat transfer performance.

This study offers the development of measurement technique to simultaneously measure the temperature and the acoustic pressure within a high-pressure environment, which is essential for a well-defined condition in the study of heat exchangers in oscillatory flow. It is anticipated that the results here will contribute to the development of the design guidelines for the heat exchangers of the next generation of thermoacoustic engines/refrigerators or Sterling engines/coolers in cryogenic applications.

## 2.0 Experimental Methods

Figure 1 shows the overview of the half-wavelength standing wave experimental setup and the measurement technique in this study. The rig is designed and constructed as a test facility for investigating the thermal and hydraulic performance of heat exchangers (without the stack or regenerator) in oscillatory flow, as relevant to the conditions in practical thermoacoustic engines and refrigerators. The setup is 8.9 m long and consists of an acoustic driver (Q-drive -1S102D), test section enclosing three T-HEX arranged in series (a hot heat exchanger centrally placed between two cold heat exchangers), 2-inch circular cross-sectional resonator, gas-charging unit, hot and cold water loops, measurement devices and data acquisition system. Helium gas is used as the working fluid in the set-up, which has a total volume of 21liters at 1bar mean pressure. The experimental rig is operated at the resonance frequency ( $f$ ) of 53.6 Hz.

### 2.1 Acoustic driver

An essential requirement in this study is to test the T-HEX sets in an oscillatory flow which is generated and sustained in the setup using a Q-drive acoustic driver (1S102D). The acoustic power output from the driver is 225 W at the maximum piston displacement of 12 mm (peak to peak), and it is powered and controlled (frequency and excitation voltage) by a power supply, Allen-Bradley model PowerFlex700, and housed in a pressure vessel that allows connection to the rest of the test rig via a flanged 2-inch 90° elbow that matches the flanged 2-inch straight resonator. The peak to peak piston stroke of the driver was monitored using Laser Displacement Sensor (LDS) LK G152 (0.25 V/mm (4mm/V)) with a measurement range of  $\pm 10.8$ V, positioned directly above the optical window in the acoustic driver housing. The resonator defines the phase of pressure and velocity of the oscillating helium gas that interacts with the boundaries of the three T-HEX in the test section.

## 2.2 Test section and heat exchangers

The test section houses the cross-flow T-HEXs, spacers, dynamic pressure transducers, Type-K thermocouples (T/C) and the insulation materials (silicate wool), while its lid accommodates the feedthrough assembly for T/C's and Swagelok fittings for transducers' cables and water tubes (cf. Figure 1). The test section is fabricated from a SCH40 SS-316 material, and its mid-point is located at a distance  $x = 4.29$  m from the pressure antinode ( $x = 0$ ). The three identical T-HEXs are arranged in series (two cold heat exchangers 'CHX1 and CHX2' and a hot heat exchanger 'HHX') to form a 'core' that is enclosed within the high-pressure environment. The geometric parameters of the T-HEX are shown in Table 1, and the two configurations that are investigated here are identified as T-HEX (flat) and T-HEX (ogive) as shown in Figure 2. T-HEX (flat) (Figure 2a) is the T-HEX with a squared edge having curvature radius (RC) of 0 mm, and the T-HEX (ogive) (Figure 2b) is the T-HEX with aerodynamic shape (ogive) having RC of 7 mm. An 'ogive' edge shape was selected for use in this study based on the knowledge of using streamlined shape to reduce drag at the boundary layer, thus minimising pressure drop.

The T-HEX are designed as water heated and water cooled compact heat exchangers, which are fabricated from a block of aluminium material that has a thermal conductivity of 180 W/m.K. On the gas side of the T-HEX, 89 circular channels 'tubes' are arranged in a triangular pitch pattern (Isosceles triangle) with 4 mm and 5.5 mm horizontal and vertical distances. Pressurised helium gas oscillates through the tubes and water flows unidirectionally through the ten rectangular channels (12 mm x 1.5 mm x 67mm each) at atmospheric pressure in a cross-flow pattern. Each T-HEX is clamped between two end-caps to allow connection to the water tubes. During the experiments, a refrigerated circulator with cooling power of 500 W (at 20°C) is used to maintain the inlet temperature of the CHX1 and CHX2 at a constant temperature of 10°C. A PID temperature controller (Omega Model

CN8592) is used to control the temperature of the hot water bath within  $\pm 1^\circ\text{C}$  accuracy at a desired HHX inlet temperature (30, 50 and  $70^\circ\text{C}$ ). A constant flow rate of 0.44 L/min is used on all the heat exchangers, and it is achieved by Swagelok needle valve and measured by a mini flow turbine with an accuracy of 0.005 l/min.

The T-HEXs are separated using four spacers to minimise the heat conduction between the heat exchangers. Two middle spacers separate the CHX1, HHX, and CHX2 with an equal gap of 4 mm, while two end spacers connect the CHX1 and CHX2 to the steel resonator. Each spacer is fabricated from Nylon 6 material (0.88 W/mK at  $25^\circ\text{C}$ ) to an inner radius of 57.4 mm and a thickness of 8.8 mm. Customised fittings for the dynamic pressure sensors and the T/C's are mounted through the spacers to facilitate simultaneous measurement of oscillating pressure and mean temperature near the heat exchangers. Pressure sensors are flush mounted (cf. Figures 1) at 6.5 mm from the nearest T-HEX.

### 2.3 Measurements

On the gas side in the setup, 20-pair of 0.5 mm diameter Type-K thermocouples (T/C's) are positioned in the high-pressure environment using a high-density feedthrough assembly (cf. Figure 1). Three T/C's are positioned near the heat exchangers at  $x = 3.44$  m, 3.84, 4.04 and 4.74 m, to measure the gas temperature, which implies that 12 T/C's (T1 – T12) are used for the gas temperature measurement around the heat exchangers. An average of three temperature readings at each location is utilised in the heat transfer calculations. T13, T14 and T15 are attached to the wall of the heat exchanger gas channels to measure the surface temperature directly, which are also employed as boundary conditions in the simulation. Additional thermocouple T16 and T17 are used to monitor the gas temperature at distance 202mm from the CHX1 side and inside the insulation material, respectively, to observe the heat transfer by conduction through helium gas and the insulation material. T18 – T23 are T/C Type K-310 of 1.0 mm diameter, installed in the water tubes (cf. Figure 1b) to obtain

temperature data from the water side. Also, T24 is used to monitor the temperature of the resonator to determine the heat loss through the resonator wall.

Several dynamic pressure transducers (P0 – P7) from PCB PIEZOTRONICS (model 112A22) are distributed along the experimental rig to measure the acoustic pressure at different locations. P0 is positioned at the pressure antinode ( $x = 0$ ) in the standing wave at the closed end in the rig. The pressure amplitude from P0 is used as the controlling parameter during the experiments and for determining the resonance frequency, i.e. the operating frequency at which the highest acoustic pressure was achieved. P1, P2, P3 and P7 are located at distances  $x = 3.44$  m, 3.84, 4.04 and 4.74 m, respectively, from the closed end. At some point, port of P3 was used interchangeably between a pressure transducer and a thermocouple. The acoustic pressure measurements from P2 and P7 are used as the acoustic boundary conditions in the simulation. The pressure amplitudes near the T-HEX are measured using P4, P5 and P6, which are installed at 32 mm apart in the high-pressure environment without exposing the sensors to the pressurised helium gas. The signal cables from P4, P5 and P6 are channelled through stainless tubes of 8 mm diameter each and the feedthrough fittings. The signal outputs (volt) from the pressure transducers are amplified using ICP signal conditioner (model 482C16). All readings (temperature, pressure, piston displacement, and water flow rates) from the sensors are transferred to the PC via data acquisition card (OMB-Daq Temp Model 14) from Omega. The pressure and displacement signals are acquired simultaneously and transformed through FFT to find the individual phases and the phase difference, which are obtained from LABVIEW programme with an accuracy of  $0.01^\circ$ .

The data collection procedure during the experiments usually starts by allowing the two water loops to first create heating and cooling loads in a typical set of heat exchangers. When the system is in a thermal equilibrium condition, the acoustic driver is switched on to excite the flow and cause the



compressed helium gas within the set-up to oscillate through the heat exchangers, thereby generating the transfer of heat between the hot and cold heat exchangers. Simultaneously, oscillating pressures are produced as the helium gas moved through the heat exchangers. When the system reaches steady oscillatory and thermal conditions, temperature and pressure amplitude data from thermocouple and pressure transducers are recorded on the gas side at every location within the test section. Similarly, for the water side, water temperatures and flow rate data are recorded. A similar procedure is involved for completing all experiments on each set of heat exchangers and edge shapes.

## 2.4 Data reduction

The measured temperatures and pressure amplitudes from the experiments are used in the heat transfer and pressure drop calculations. The heat transfer rate ( $\dot{Q}$ ) can be calculated from:

$$\begin{aligned}\dot{Q}_h &= \rho_w q_v c_{p,w} (T_{w,i} - T_{w,o})_h \\ \dot{Q}_{c1,c2} &= \rho_w q_v c_{p,w} (T_{w,o} - T_{w,i})_{c1,c2}\end{aligned}\tag{1}$$

where  $\rho_w$ ,  $q_v$  and  $c_p$ , are the water density (Maidment, 1993), volume flow rate and specific heat capacity (Richardson, 2005) of water, evaluated using the average of water inlet and outlet temperatures  $(T_{w,in} + T_{w,out})/2$ . The heat loss ( $\dot{Q}_{loss}$ ) in the experiment is evaluated to ensure the accuracy of the heat transfer calculations. Before every experiment, a static measurement (i.e. no flow excitation) was conducted to evaluate heat loss by conduction, when the system is in a thermal equilibrium condition. The heat transferred to or removed from the gas is evaluated using the temperature difference between the water inlet and outlet of each heat exchangers, which is attributed to the heat transfer by conduction since there was no flow excitation. The maximum of these values is 15.59, 29.19 and 17.17 W for CHX1,

HHX, and CHX2, respectively, at HHX inlet temperature ( $T_h$ ) of 70°C and CHX1 and CHX2 inlet temperatures ( $T_{c1,c2}$ ) of 10°C. Also, heat loss through the insulation material is evaluated using Fourier equation,  $\dot{Q}_{loss} = k_{ins} A_{hx} (\Delta T_{ins} / \Delta x)$ , where  $k_{ins}$ ,  $A_{hx}$ ,  $\Delta T_{ins}$  and  $\Delta x$  are the thermal conductivity of insulation, HEX outer surface area, temperature difference and the thickness of insulation. Additional heat loss through helium gas is also monitored at a distance 202 mm from CHX1 (cf. Figure 1). The heat transfer rates through the insulation material and the helium gas are 102.4 mW and 14 mW, respectively (at  $T_{c1,c2} = 10^\circ\text{C}$  and  $T_h = 70^\circ\text{C}$ ). During the heat transfer analysis, the estimated heat leaks are subtracted from the heat transfer rates. Other sources of heat leak include the heat conduction through the fittings. However, this is difficult to account for and considered negligible in this study.

The convective heat transfer coefficient,  $h$ , on the gas side of the heat exchangers are determined as (Tang et al., 2013; Al-Damook et al., 2015):

$$h_{h,c1,c2} = \frac{\dot{Q}_{h,c1,c2}}{A_s \left[ T_s - \left( \frac{T_{g,in} + T_{g,out}}{2} \right) \right]} \quad (2)$$

where  $\dot{Q}$ ,  $(T_{g,in} + T_{g,out}) / 2 = T_i$  is the heat transfer rates,  $T_{g,in}$  and  $T_{g,out}$  are the gas temperatures at the inlet and outlet of the heat exchangers gas channel.  $T_i$  is the mean gas temperatures at the locations near the heat exchangers (cf. Figure 1).  $T_s$  is the measured surface temperature of the gas channel. Subscripts  $h$ ,  $c1$ , and  $c2$  denote the heat transfer conditions for the HHX, CHX1 and CHX2. The expression in the square bracket in equation (2) is often referred to as the thermal potential for the heat transfer coefficient. In oscillatory flow, the thermal potential is application dependent (Zhao and Cheng, 1995; Brewster et al., 1997; Shi et al., 2010) and it is defined here to reflect the contribution of the gas temperatures

at the inlet and outlet vicinity of the T-HEX gas channel. The Nusselt number ( $Nu$ ) is related to the heat transfer coefficient ( $h$ ) in the following expression as:

$$Nu_{h,c1,c2} = \frac{hd_h}{k} \quad (3)$$

where  $d_h$  is the hydraulic diameter.

The drive ratio ( $DR$ ) constitutes a parameter by which the intensity of thermoacoustic oscillations is evaluated in practical thermoacoustic systems (Swift, 2002; Piccolo 2011; Tijani and Spoelstra, 2011) and is described by:

$$DR = \frac{|p_o|}{p_m} \times 100\% \quad (4)$$

In the experiments, the  $DR$  is controlled by varying the excitation voltage that is supplied to the acoustic driver at a fixed mean pressure and resonance frequency, which in turn changes the gas parcel displacement amplitude ( $\xi_1$ ) accordingly. The  $\xi_1$  can be converted to acoustic velocity ( $u_1$ ) and vice versa using  $\xi_1 = |u_1|/\omega$ , with the velocity leading the displacement by  $90^\circ$  in phase. Therefore, the relationship between the  $DR$  and  $\xi_1$ , for an ideal gas behaviour, can be expressed as (Swift, 2002):

$$\xi_1 = \frac{aDR}{\omega} \sin(k'x) \quad (5)$$

where  $a$ ,  $\omega$ ,  $k'$ , and  $x$  are the speed of sound, angular frequency, angular wave number, and the distance (in the direction of wave propagation) from the pressure anti-node ( $x = 0$ ). Other important parameters that influence the heat transfer are the thermal ( $\delta_k$ ) and viscous ( $\delta_v$ ) penetration depths which are defined as:

$$\delta_k = \sqrt{\frac{2k}{\omega\rho c_p}}, \quad \delta_v = \sqrt{\frac{2\mu}{\omega\rho}} \quad (6)$$

where  $k$ ,  $\mu$ ,  $\rho$  and  $c_p$  are the thermal conductivity, dynamic viscosity, the density and specific heat capacity of helium gas. The thermal and viscous penetration depths are 0.46 – 0.56 mm and 0.38 – 0.46 mm, respectively, for the range of operating temperatures in the experiments and the simulation (10 – 150°C). The Prandtl number can be expressed as  $Pr = (\delta_v / \delta_k)^2 = \mu c_p / k$ , which gives a value of approximately 0.68 at an average value of the penetration depths. The acoustic Reynolds number is defined based on hydraulic diameter as:

$$Re_1 = \frac{\rho u_{m,h} d_h}{\mu} \quad (7)$$

where  $u_{m,h}$  is the velocity amplitude at the centre of the HHX ( $x = 4.29$  m), obtained from  $u_{m,h} = u_1 / \sigma$ , where  $\sigma$  is porosity of the heat exchanger defined as  $\sigma = A_o / A_{fr} \cdot A_o$  and  $A_{fr}$  are the cross-sectional area of the gas flow channel and the total frontal core area of the heat exchangers, respectively (Wakeland and Keolian, 2004; Tang et al., 2014). The temperature-dependent thermal conductivity ( $k$ ) and viscosity ( $\mu$ ) of helium are evaluated as (Swift, 2002):

$$k = 0.152 \cdot \left( \frac{T}{T_o} \right)^{0.72}, \quad \mu = 1.99 \cdot 10^{-5} \cdot \left( \frac{T}{T_o} \right)^{0.68} \quad (8)$$

The density is defined following an ideal gas law as,  $\rho_m = P_m / RT$ , where  $R$  is the specific gas constant. Following Swift (2002) and Marx et al. (2004), the pressure drop due to minor losses in oscillatory flow is defined as:

$$\Delta P = \frac{1}{2} K \rho_m u_1^2 \quad (9)$$

where  $K$  is the minor loss coefficient, which has been shown to depend on the flow direction within an acoustic flow cycle (Morris et al., 2004; Petculescu and Wilen, 2003).

The measurement uncertainty in the experimental result is evaluated based on the approach described in the literature (Moffat, 1988; Adams, 2002; Dieck et al., 2005). The temperatures on both the gas and water sides of the heat exchangers are measured with a relative uncertainty of 0.2°C. The error bars on the heat flux and Nusselt number calculations, as will be discussed later, are determined based on this method and represent combined uncertainties of 12.5% and 12.6%, respectively. The uncertainties from the geometric tolerance of the heat exchanger fabrication and thermal conductivity of helium are assumed negligible.

### 3.0 Numerical methods

#### 3.1 Model Description and Methodology

The 3D models of the T-HEX (flat) and T-HEX (ogive) are developed in ANSYS Fluent 17.0 (2015). Figure 3 shows the method of integrating the experiments with the CFD model. The modelling phase begins with the development of a 2D model (Ilori et al., 2014) based on the data from the literature. From this 2D model, it was established that the computational domain of 0.9 m is sufficiently long to prevent the influence of the upstream and downstream flow conditions on the flow structures near the heat exchangers. Subsequently, the experimental set-up is developed, and data are collected, which are then used for the boundary and initial conditions and the result validation.

### 3.2 Computational domain and solution procedure

The inlet ( $x = 3.84$  m) and outlet ( $x = 4.74$  m) of the 0.9 m computational domain, as shown in Figure 4a, correspond to the locations of P2 and P7 in the experimental set-up (cf. Figure 1). For meshing purposes, the domain is decomposed into three segments, consisting of the HEX-core, the upstream and the downstream sections. Figures 4b and c show the unstructured mesh in the HEX-core and the structured mesh in the other sections. Figure 5 shows the general procedure for achieving the simulation results. The ovals and boxes in the middle of the flow chart represent the main workflow within the solver. Calculations start at an assigned time step size ( $\Delta t$ ), which must be chosen small enough to achieve the desired accuracy and avoid numerical divergence. The  $\Delta t$  is defined as:

$$\Delta t = \frac{1}{Nf} \quad (10)$$

where  $N$  is the number of time steps over one flow cycle, which is found to be 600 after the sensitivity check on the time discretisation. The mesh quality is assessed through the maximum skewness, minimum orthogonal quality and aspect ratio, with values of 0.7, 0.3, and 22.1, respectively, which are well within the acceptable range (ANSYS 17, 2015) and allowed the simulation results to converge based on the chosen criteria, as discussed in the next section.

### 3.3 Physical model

The unsteady flow fields are solved using 3D Navier-Stokes equations (ANSYS Fluent 17, 2015; Versteeg and Malalasekera, 2007). Buoyancy effect is considered in the simulation, and the Reynolds-Averaged Navier-Stokes (RANS) equation is used for the turbulence model closure. Previous relevant studies (Mohd Saat, 2013, 2017) have used RANS equations to model turbulent flow through the heat exchangers in oscillatory flow. The RANS equations

are derived from Navier-Stokes equations by time averaging the transport and energy equations, with variables decomposed into mean and fluctuating components,  $\varphi = \bar{\varphi} + \varphi'$ , where  $\bar{\varphi}$  and  $\varphi'$  are the mean and fluctuating components of the scalar variable such as velocity, pressure, etc. In conservative form, the RANS equations can be written for the continuity, momentum and energy equations as:

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_j} (\rho u_j) = 0 \quad (11)$$

$$\frac{\partial (\rho u_i)}{\partial t} + \frac{\partial (\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + F_i + \frac{\partial}{\partial x_j} (\tau_{uj})_{eff} + \frac{\partial}{\partial x_j} (-\overline{\rho u'_i u'_j}) + \frac{\partial}{\partial x_i} (-\overline{\rho u'^2}) + S_m \quad (12)$$

$$\frac{\partial (\rho E)}{\partial t} + \frac{\partial}{\partial x_i} [u_i (\rho E + p)] = \frac{\partial}{\partial x_j} \left( (k)_{eff} \frac{\partial T}{\partial x_j} + u_i (\tau_{uj})_{eff} \right) + S_h \quad (13)$$

where  $F$ ,  $S_m$  and  $S_h$  are the external force, and source terms.  $(\tau_{uj})_{eff}$  and  $-\overline{\rho u'_i u'_j}$  are the effective stress tensor, and Reynolds Stresses term used to model momentum equation for the turbulence affected flow, and they are defined as:

$$(\tau_{uj})_{eff} = \mu \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) - \frac{2}{3} \mu_{eff} \frac{\partial u_k}{\partial x_k} \delta_{ij} \quad (14)$$

$$-\overline{\rho u'_i u'_j} = \mu_t \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) - \frac{2}{3} \left( \rho \kappa + \mu_t \frac{\partial u_k}{\partial x_k} \right) \delta_{ij} \quad (15)$$

Shear Stress Transport (SST)  $k-\omega$  turbulence model (Menter, 1994) is used for turbulence closure, which has been shown to predict the oscillating velocity profiles near the wall and the core, better than the other turbulence models when compared with the experimental data (Mohd Saat, 2013, 2017). The choice of turbulence model against the laminar model for this study is discussed in section 4.0. Pressure-based solver, Pressure Implicit Splitting Operators (PISO) algorithm, and second-order discretisation are used for the transport and turbulent equations in all simulation cases. The convergence criteria of  $10^{-5}$  and  $10^{-8}$  are used for the

transport and energy equations, respectively. Default values are retained for all other constants in the SST k- $\omega$  turbulence model (ANSYS Fluent 17.0, 2015; Tasmin and Fraser, 2010).

### 3.4 Boundary and initial conditions

The pressure amplitudes and phases measured by P2 and P7 (cf. Figure 4) are assigned to the domain inlet and outlet as the acoustic boundary conditions which are described by:

$$p_{in} = p_{1,in} \cdot \cos(\omega t + \phi_{in}) \quad (16)$$

$$p_{out} = p_{1,out} \cdot \cos(\omega t + \phi_{out}) \quad (17)$$

where  $p_{1,in}$ ,  $p_{1,out}$ ,  $\phi_{in}$  and  $\phi_{out}$  are the measured pressure amplitudes and their corresponding phases. The turbulence conditions at the domain inlet and outlet are specified in terms of the intensity and length scale as:

$$I = 0.16(\text{Re}_{1(in,out)})^{-1/8} \quad \ell = 0.07D \quad (18)$$

The acoustic Reynolds number is defined as  $\text{Re}_{1(in,out)} = \rho_o u_{1(in,out)} D / \mu_o$  for the domain inlet and outlet locations. The acoustic velocities in the  $\text{Re}_{1(in,out)}$  is calculated as:

$$u_{1,in}(x) = \frac{p_o}{\rho_m a} \sin(k' x_{in}) \quad (19)$$

$$u_{1,out}(x) = \frac{p_o}{\rho_m a} \sin(k' x_{out}) \quad (20)$$

The value of density and dynamic viscosity at the reference temperature (300 K) are used in equations (19) and (20).  $p_o$  is the measured pressure amplitude at the antinode. The thermal boundary conditions on the CHX1, HHX and CHX2 walls are specified as constant wall temperatures, which are measured from the experiments. At the inlet and outlet of the



domain, additional temperature conditions  $\partial T / \partial x|_{x_{in}, x_{out}} = 0$  are specified such that the temperature of the cells next to the boundaries is equal to that of the reversing flow. The resonator wall is modelled as adiabatic and non-slip boundary conditions are applied to all walls in the model.

#### 4.0 Results and Discussion

The results in this section are arranged into eight sub-sections. Section 4.1 discusses the pressure amplitude obtained at different axial locations. Sections 4.2, 4.3 and 4.4 focus on the temperature, heat flux and Nusselt number, respectively, at various  $DR$ . Section 4.5 discusses the dependency of  $Nu$  on different  $T_h$ . Section 4.6 compares the numerical  $Nu$  with the models from the literature, while Section 4.7 discusses further simulation results to extend the understanding of the heat transfer and pressure drop in oscillatory flow. The simulation results are obtained within a flow cycle as shown in Figure 6. A flow cycle is discretized into 20 equal phases ( $\phi$ ) of which  $\phi 1$ -  $\phi 10$  constitute the suction stage, and  $\phi 11$  to  $\phi 20$  represent the ejection stage.

To build confidence in the numerical results, a systematic mesh convergence study was carried out using T-HEX (ogive). A very fine mesh size ( $< 0.12$  mm) was required in the gas channels for accurate resolution of the flow phenomena, which led to a maximum improvement of less than 1% between the ‘coarse’ and the ‘fine’ mesh size at the refinement ratio of 1.8. The mesh resolution is sufficient to achieve mesh-independent results (Roache, 1994; Ilori et al., 2014). Every simulation case involved about 4.5 million mesh cells (with more than 98% located in the region occupied by the heat exchangers) and simulation run of more than 90,000 timesteps, representing a real time of 2.8 seconds.

#### 4.1 Pressure amplitude profile

Figure 7 shows the comparison of pressure amplitude distribution in the region between  $4.2\text{m} < x < 4.4\text{m}$  (marked with a dashed line in Figure 4) for measured (symbols) and numerical (solid lines) results. In all the plots, it can be observed that the pressure profile is distorted around the heat exchangers at  $x = 4.244, 4.276, 4.308$  and  $4.340\text{ m}$ , which is due to the flow resistance caused by the sudden change in the cross-section of the flow channel. It should be noted that the pressure profiles are asymmetrical, which is because the centre of HHX ( $x = 4.29\text{ m}$ ) did not coincide with the centre of the test rig ( $x = 4.45$ ) where the velocity is nonzero (velocity antinode or pressure node). Therefore, the pressure profile at  $0 < x < 4.29\text{ m}$  is on the rising side of the standing wave, which makes it higher than the profile at  $4.29 < x < 4.45\text{ m}$ . In a standing wave thermoacoustic system, the internal elements (heat exchangers and stack) must be placed at a location where the oscillating pressure and velocity are non-zero.

The choice of a suitable viscous model for every simulation case at a specific  $DR$  is important to achieve accurate numerical predictions. For this reason, simulation cases for laminar and turbulence models were first performed. Figure 7a shows the pressure amplitudes from both simulation and experiments for T-HEX (Flat) at  $T_h = 70^\circ\text{C}$ , which reveal that the turbulence model gave better agreement with the experimental data than the laminar model, noticeably in the vicinity of the heat exchangers. The acoustic pressure from the laminar model deviates increasingly from the experiment results as the  $DR$  increases, which suggests that the turbulence model well resolves the complex flow behaviour around the heat exchangers. Mohd Saat (2013, 2017) obtains a similar result for a parallel-plate structure, where the turbulence models yielded results that agreed well with the experimental data than the laminar model counterpart. Also, Merlki and Thomann (1975) suggested that the flow regime in oscillatory flow should be considered laminar if the critical Stokes Reynolds number (

$Re_c = 2u_{m,h}/(\nu\omega)^{1/2}$ , where  $\nu$  is the kinematic viscosity) is less than 400. Table 3 shows the  $Re_c$  in the experiments for T-HEX (flat) at  $T_h = 70^\circ\text{C}$ . At  $DR \leq 0.64\%$ , the  $Re_c$  is lower than the suggested transition regime, while at  $DR > 0.64\%$  the  $Re_c$  is greater. In this paper, a turbulence model is used in all the simulation cases based on the comparison between the turbulence and laminar models against experimental data (cf. Figure 7a), which favoured the use of the former.

Figures 7b and c show the experimental and numerical results for two different thermal conditions on T-HEX (flat), the adiabatic and the imposed temperature-gradient conditions. In the adiabatic condition, the heat exchanger walls are considered as adiabatic to mimic the experiments where the heat exchangers are tested at room conditions with no imposed temperature difference, mainly to serve as a reference for result comparison. For the imposed temperature gradient condition, the CHX1, CHX2 are maintained at  $T_{c1,c2} = 10^\circ\text{C}$ , and HHX is kept at  $T_h = 70^\circ\text{C}$  to allow direct comparison with the experimental data. In both plots (Fig. 7b and c), there are good agreements between the numerical and experimental results with averaged discrepancies of less than 5% at the maximum  $DR$ . Figure 7d shows the measured and numerical results for T-HEX (ogive). Like Figures 7b and c, a good agreement can be seen in the plot, with an average discrepancy of less than 10% at the highest  $DR$ . The agreement between the measurement and simulation results is needed to yield confidence in the simulation results.

The influence of the edge shape on the pressure amplitude profile can be examined by comparing the simulation results in Figures 7c and d. It can be observed that the magnitude of distortion of pressure profile near the heat exchangers is different considerably for the two geometries. In both cases, the distortion is highest at  $x = 4.276$  m and  $x = 4.308$  m, which corresponds to the gaps between CHX1/HHX and HHX/CHX2, respectively. The ogive edge

minimised the pressure drop by 70 and 185 Pa, respectively, at both locations for  $DR = 1.29\%$ . It can be observed from the plot that the minimisation of pressure drop by the aerodynamic shape gets significant as the  $DR$  increases, which indicates that the nonlinear effect such as vortex formation and shedding, is increasingly minimised, as will be discussed in section 4.7. This is quite interesting from the viewpoint of a practical thermoacoustic system which often operates at high amplitudes ( $DR > 5\%$ ) (Backhaus and Swift, 2000; Tijani and Spoelstra, 2011).

#### 4.2 Temperature profile

In Figure 8, the difference between the experimental and simulation gas temperatures are presented for various locations near the heat exchangers ( $x = 4.244, 4.276, 4.308$  m and  $4.340$  m). There exists a good agreement between both results with maximum discrepancies of  $6.7\%$  and  $5.3\%$  for T-HEX (flat) and T-HEX (ogive), respectively. The difference occurs at the low  $DR$  ( $< 0.31\%$ ), where the gas displacement and the imposed temperature gradient are low. It should be noted that the difference between  $T_h$  and  $T_{c1,c2}$  (i.e.  $T_h - T_{c1,c2}$ ) is used as a reference in the evaluation of the deviation. In both plots, the numerical temperature profile shows a similar trend to the experiments, with rapid decrease/increase in the hot/cold gas temperature at  $DR \leq 0.64\%$ , which indicates rapid movement of the hot gas from the hot region to the cold region. In both cases, the measured CHX1 and CHX2 temperatures are higher in magnitude than the numerical values, while the measured HHX temperatures are lower than the numerical at  $DR < 0.65\%$ . Above this point, both results are almost the same for CHX1 and CHX2 as well as for the HHX for the two configurations.

The influence of the heat exchangers edge shape on the gas temperatures can be discussed from Figure 8a and b. In the plots, the predicted gas temperatures for T-HEX (ogive) are higher for HHX and lower for CHX1 and CHX2 at the investigated  $DR$ , in comparison with

the T-HEX (flat), the maximum difference of about 3°C (i.e. 4% at a reference temperature difference  $T_h - T_{c1,c2}$ ).

### 4.3 Heat flux ( $q$ )

In the simulation, the heat flux is obtained as a function of both space and cycle (Zhao and Cheng, 1995; Shi et al., 2010; ANSYS Fluent 17.0, 2015), which can be defined as:

$$q_{h,c1,c2} = \frac{1}{2\pi A_s} \int_0^{2\pi} \int_{A_s} q(x, \phi) \big|_{wall} dA d\phi \quad (21)$$

The local instantaneous heat flux,  $q(x, \phi)$ , as a function of area and phase are obtained directly from simulation result and then averaged over a flow cycle. Figure 9 shows the comparison between the experimental and numerical heat fluxes for the two heat exchanger types. The positive heat fluxes reflect the heat being transferred from HHX wall to the oscillating gas while the opposite is the heat transfer from the gas to the CHXs wall. There are good agreements between the experimental and the numerical heat fluxes which is, however, better at  $DR < 0.64\%$  than at higher  $DR$ 's. The trend from both results is similar, with a gradual increase in the heat fluxes. The increase or decrease of  $DR$  reflects the increase or decrease in the gas displacement amplitude (cf. Equation 5). A similar effect of  $DR$  on heat transfer was observed by Piccolo (2011), where a variation of heat flux (heat load per unit area) as a function  $DR$  is reported through a numerical study.

The comparison between the numerical results in Figure 9a and b shows that the T-HEX (ogive) yielded lower heat fluxes noticeably at  $DR < 0.8\%$ . However, as the  $DR$  increases, the difference between the heat fluxes for the two edge shapes becomes less pronounced, which are 15.67 and 15.15 kW/m<sup>2</sup> at  $DR = 1.29$ . According to the heat balance from the symmetric arrangement of the heat exchangers,  $\dot{Q}_h = \dot{Q}_{c1} + \dot{Q}_{c2}$ , the magnitude of heat absorbed by the CHXs is higher than the heat supplied to the oscillating gas by the HHX with a maximum

difference of 3.3% and 2.5% for T-HEX (flat) and T-HEX (ogive), respectively. This deviation in the heat input and the heat removed may be attributed to the nonlinear effects such as streaming, which can advect heat away from the heat exchangers. The magnitude of the heat imbalance is lower for the T-HEX (ogive) and suggests this fact. The result here is very interest considering that the heat transfer performance of both edge shapes become increasingly similar as the  $DR$  increases. Meanwhile, the ogive shape further shows an increasing performance regarding the pressure drop as will be seen later.

#### 4.4 Nusselt number ( $Nu$ )

Like the heat flux in section 4.3, the  $Nu$  in equation (3) is presented as a function of flow cycle and the heat exchanger area in contact with the oscillating gas as:

$$Nu_{h,c1,c2} = \frac{1}{2\pi A_s} \int_0^{2\pi} \int_{A_s} Nu(x, \phi) dA d\phi; \quad Nu(x, \phi) = \frac{h_c(x, \phi) d_h}{k} \quad (22)$$

where  $Nu(x, \phi)$  and  $h_c$  are the local instantaneous  $Nu$  and the heat transfer coefficient defined as:

$$h_c(x, \phi) = \frac{q(x, \phi)}{\Delta T(x, \phi)} \quad (23)$$

The thermal potential for the heat transfer coefficient is defined in terms of space and time as

$\Delta T(x, \phi) = T_s(x) - T_i(\phi)$ .  $T_i(\phi)$  is the mean of gas temperatures defined as:

$T_i(\phi) = (T_{g,in}(\phi) + T_{g,out}(\phi))/2$ , where  $T_{g,in}(\phi)$  and  $T_{g,out}(\phi)$  are the inlet and outlet

instantaneous gas temperatures of the heat exchangers.

Figure10 shows the  $Nu$  comparison for T-HEX (flat) and T-HEX (ogive). Both measured (symbols) and numerical (solid line) results have a similar increasing trend with an increase in the  $DR$ . At low  $DR < 0.6\%$ , the numerical model slightly underpredicts the heat transfer,

whereas, it overpredicts the performance at higher amplitudes ( $DR > 0.6\%$ ). The result is consistent with the findings in the literature (Piccolo, 2011). However, the magnitude of deviation of both low and high amplitude in the current study is considerably lower. It should be noted that since the heat exchangers are identical, it is quite interesting to have similar trends in the  $Nu$  for CHX1, HHX and CHX2 in both results. The average discrepancies between the experimental and numerical results are 18% and 23% for T-HEX (flat) and T-HEX (ogive), respectively. The deviation in the results may be attributed to few factors which may include the method of heat transfer evaluation in the simulation, the model capability to resolve the complex flow phenomena, and thermoacoustic effect in the physical experiments.

#### 4.5 Effect of temperature on the $Nu$

Figure 11 shows the change in  $Nu$  against  $DR$  due to temperature. The temperature on HHX ( $T_h$ ) is varied from 30 – 70°C at 20°C step in both experiment and simulation. T-HEX (flat) is used for the investigation. In both cases, a similar trend can be observed with a uniform increase in  $Nu$  over the  $DR$  as the  $T_h$  increases, which is more pronounced in the experimental result. The observed increase in the  $Nu$  can be attributed to the change in the temperature dependent properties of the working fluid such as the viscosity, density and the heat capacity. Also, since the heat exchangers interact thermoacoustically with the oscillating flow, acoustic energy is generated/consumed due to thermoacoustic/thermoviscous effects with thermal energy as well.

#### 4.6 Comparison of $Nu$ against previous studies

Figure 12 shows the comparison between the current numerical heat transfer result and the existing models in the literature. For the comparison, the  $Nu$  for T-HEX (flat) at  $T_h = 70^\circ\text{C}$  are compared against the acoustic Reynolds number. The existing correlations that are considered include the Time-Average Steady-Flow Equivalent (TASFE) model (Richardson, 1967) and the experimental correlation proposed by Nsofor et al. (2007). The  $Nu$  and acoustic

Reynolds number (cf. equations 3 and 7) from the selected studies are calculated based on the same length scale ( $d_h$ ). Piccolo and Pistone (2006) presented  $Nu$  correlation for the TASFE model as:

$$Nu = \frac{\varpi}{\pi} \int_0^{\frac{\varpi}{\pi}} \left\{ 3.66 + \frac{0.0668(d_h/l) \text{Pr Re}_1 \sin \omega t}{1 + 0.04[(d_h/l) \text{Pr Re}_1 \sin \omega t]^{2/3}} \right\} dt \quad (24)$$

Nsofor et al. (2007) correlated their experimental data in terms of  $Nu$  defined based on the RMSRe ( $\text{Re}_{rms} = \text{Re}_1/\sqrt{2}$ ), for heat transfer performance of a finned-tube type heat exchanger of a thermoacoustic refrigeration system, which can be written as:

$$Nu = 0.61(\text{Re}_1/\sqrt{2})^{0.31} \text{Pr}^{0.11} \quad (25)$$

The TASFE approximation is based on a steady flow and may reflect the increase in  $Nu$  with an increase in the acoustic Reynolds number. The results in Figures 12 reveal that the current CFD model and TASFE approximations predicted higher  $Nu$  by 24.9% and 35.0%, respectively, in comparison with the experimental correlation of Nsofor et al. (2007). The TASFE model has been reported with a similar deviation by Piccolo and Pistone (2006). However, the observed discrepancy of the current numerical model may be attributed to the difference in the type of geometries. The CFD model is based on the Tube Heat exchanger type, while Finned tube type was utilised in the experiment of Nsofor et al. (2007). Also, the range of operating conditions and differences in the methods of evaluation could contribute to the difference.

#### 4.7 Numerical predictions

The numerical investigations to extend the knowledge from the experimental results are discussed in this section. The maximum velocity amplitude, flow structure, Nusselt number,



and pressure drop due to minor losses are discussed. The results are discussed for the suction stage of the flow cycle for brevity.

The maximum velocity amplitudes for T-HEX (flat) and T-HEX (ogive) are shown in Figure 13. The comparison is made at  $x = 4.32$  m to demonstrate the influence of the edge shape on flow conditions near the velocity antinode ( $x = 0.2472 \lambda$ ). In principle, other locations near the heat exchangers can be chosen to demonstrate the geometric effect on velocity amplitude. Figure 13a shows the velocity amplitudes at  $T_h = 70^\circ\text{C}$ , which increase monotonically for both heat exchanger configurations, but with higher magnitudes for T-HEX (flat) at all  $DR$ 's. The higher velocity amplitude in the case of T-HEX (flat) can be attributed to the fact that the flow transition over the  $90^\circ$  edge will be more sudden at the change in cross-section, which causes an increase in the gas velocity due to a smaller flow area (in comparison to ogive edge), according to the law of mass conservation. On the other hand, the transition of flow over a streamlined body is more gradual and lead to a smaller increase in the gas velocity. The displacement amplitudes that correspond to the velocity amplitudes in Figure 13 are in the range of 14.17 – 93.50 mm and 8.37 – 62.63 mm for T-HEX (flat) and T-HEX (ogive), respectively. The effective length of the heat exchanger is 28 mm which corresponds to the  $DR = 0.31\%$  and  $0.48\%$  for T-HEX (flat) and T-HEX (ogive), respectively. Figure 13b shows the effect of  $T_h$  on the velocity amplitudes at  $DR = 1.29$  for the two investigated configurations. The increase in the gas temperature causes an increase in the gas velocity amplitude, which appears to be linear for both edge shapes over in the investigated temperature range ( $T_h = 30 - 150^\circ\text{C}$ ). The increase in the gas velocity can be explained from the viewpoint that the fluid viscosity gets lower as the temperature increases and the gas experiences lesser viscous drag which causes it to move faster for a fixed acoustic excitation.

The vorticity contours can be used to further illustrate the effect of edge shape on flow structure around the heat exchangers. Figure 14 shows the vorticity plots in the  $x - y$  plane

(cf. Figure 4) to show the vortex structure within the gap between two adjacent heat exchangers and the edge of the CHX2 open to the resonator. The vorticity is calculated as  $\omega = \partial v / \partial x - \partial u / \partial y$ , where  $u$  and  $v$  are the velocity components in the  $x - y$  plane. Vorticity plots at  $\phi 2$ ,  $\phi 5$  and  $\phi 8$  in the suction stage of flow cycle at  $DR = 0.64\%$  are used for the comparison. At each phase, a pair of vortex structures of equal size but opposite strength is formed in the flow channel and remain attached. They are symmetrical about the centreline of the channel in the  $x-y$  plane. At the end of the channel (right side of CHX2), it can be observed that the formation of vortex structure is delayed and the strength is minimised for T-HEX (ogive) at all the three phases when compared with the T-HEX (flat). The vortex structures appearing in the ‘wake’ of the heat exchanger can create a disturbance when it is pushed back into the gas channel by the reversing flow during the ejection stage. The higher the vortex strength, the greater the disturbance and the dissipation that will be created in the flow channel. The presence of profile edge (ogive) minimised the vortex formation and shedding as well as flow velocity (cf. Figure 13) at the entrance and exit of the HEX flow channel, which led to a reduction in the pressure drop that will be discussed in the later section. There is also a smoother transition of flow structure at the gap between two adjacent heat exchangers with ogive shape. Vortices have been shown to induce streaming which in turn had an adverse impact on the efficiency of thermoacoustic systems (Oslon and Swift, 1997; Gu et al., 2012).

Figure 15 shows the dependence of  $Nu$  on thermal conditions at various  $DR$ . The results indicates a rapid increase in the  $Nu$  as the  $T_h$  increases to about  $100^\circ\text{C}$  after which it becomes gradual. The variation, however, does not show a significant dependence on the  $DR$  at  $T_h < 70^\circ\text{C}$ , which indicates that the heat transfer in this threshold is mainly due to the thermal excitation rather than the acoustic excitation. At  $T_h > 70^\circ\text{C}$ , the contribution of the acoustic excitation to the heat transfer increases, especially at the cold heat exchangers and more

significantly for the T-HEX (ogive). The highest heat transfer is achieved at  $DR = 0.64\%$  ( $T_h = 100^\circ\text{C}$ ) with the T-HEX (flat) having a 2.5% higher performance. However, on the HHX, the performance of the two heat exchangers are very similar, especially at low acoustic excitation range. The results further support the fact that the heat exchangers interact thermoacoustically with the flow and both acoustic and thermal energies contribute to the heat transfer. It is interesting that the T-HEX (ogive) shows a heat transfer performance comparable to that of T-HEX (flat).

Figure 16 shows the pressure drop ( $\Delta p$ ) due to minor losses (cf. equation 9) across the heat exchangers. The influence of edge shapes and  $DR$  on  $\Delta p$  at various thermal conditions (30 – 150°C) are considered, including the adiabatic condition which is added in the plot for reference. The pressure amplitudes are the static oscillating pressure in the fluid domain. The results are presented for the suction stage in the flow cycle (cf. Figure 6) for brevity. Figures 16a – c represent the pressure drop across the T-HEX (flat) set while Figures 16d – f denote that of T-HEX (ogive). From the plots, the pressure drop shows a dependency on the  $DR$  and edge shape for all thermal conditions. As the drive ratio is increasing, the pressure drop increases significantly due to the increasing flow complexities such as the minor losses created by the sudden change in cross section of the flow channels. This can be observed for the two edge shapes with a higher magnitude for the T-HEX (flat). Clearly, from the plots (Figure 16), the T-HEX (ogive) has pressure drop magnitude that is 43% lower for CHX2 at  $DR = 1.29\%$  and  $T_h = 70^\circ\text{C}$ . The effect of  $T_h$  can also be seen in the plots, which is more pronounced for the HHX at  $DR > 0.31\%$  due to the increase in temperature, but less for the CHX's because of the constant temperature. Due to the symmetry of the heat exchanger arrangement, the  $\Delta p$  across HHX does not differ considerably for the two edge shapes, though the ogive edge shape still has lower magnitude. The increase in temperature increases

the pressure drop due to change in the fluid viscosity which in turn causes an increase in the gas velocity, hence increased non-linearity in the flow (cf. Figure 14).

It should be noted that the pressure drop is dependent on the sampling location, as it exists in a standing wave because the ratio of kinetic energy (velocity amplitude) to the potential energy (pressure amplitude) is a function of the position in the setup. However, since the same locations are used for the comparison in the current study, the results thus reflect the role of ogive edge shape in the minimising the pressure drop across the heat exchangers, especially, at high acoustic amplitudes.

## 5.0 Conclusions

This paper investigates the characterisation of Tube-Heat Exchangers (T-HEX) in oscillatory flow, using experimental and numerical methods. A 3D computational model has been developed and validated based on the purpose-built experimental setup. Good agreement between the experimental and numerical results are achieved. The heat transfer and pressure drop performance of T-HEX show dependency on  $DR$ , HHX inlet temperature ( $T_h$ ) and edge shape of the gas channel, as observed in both experimental and numerical results. It is observed that the presence of profile edge shape causes a slight adverse reduction in the heat transfer performance at low  $DR$ . However, the effect diminishes gradually as the  $DR$  increases, and a comparable performance is observed for the two edge shapes at high amplitudes. The presence of ogive edge minimised the vortex formation and shedding as well as flow velocity at the entrance and exit of the HEX gas channels, which led to a significant reduction in the pressure drop, especially, at high amplitudes. The result here is interesting from the viewpoint of the practical thermoacoustic engines and coolers, which often operates at high amplitudes ( $DR > 5\%$ ). It demonstrates the possibility of using the heat exchanger edge shapes to minimise the pressure drop (due to minor losses) without affecting the heat

transfer and shows that the use of Tube-Heat-Exchanger with profiled gas channels (T-HEX (ogive)) will be beneficial to the overall performance of thermoacoustic systems.

### **Acknowledgement**

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# List of tables

**Table 1:** Heat exchangers geometric parameters

Helium gas side	T-HEX
Effective flow length, mm	28
Number circular tubes	89
Tube diameter ( $d_t$ ), mm	3
Frontal core diameter ( $f_c$ ), mm	57.4
Porosity ( $\sigma$ ), %	24.31
Separation wall thickness, mm	0.5
Effective heat transfer area	
- T-HEX (flat), m <sup>2</sup>	0.0273
- T-HEX (ogive), m <sup>2</sup>	0.0259

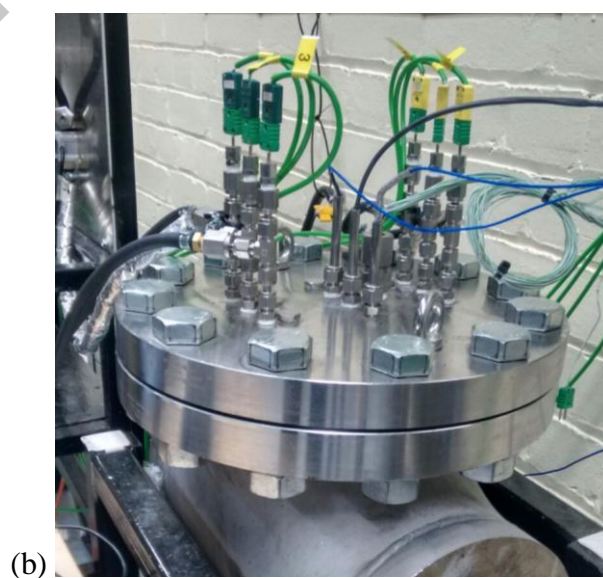
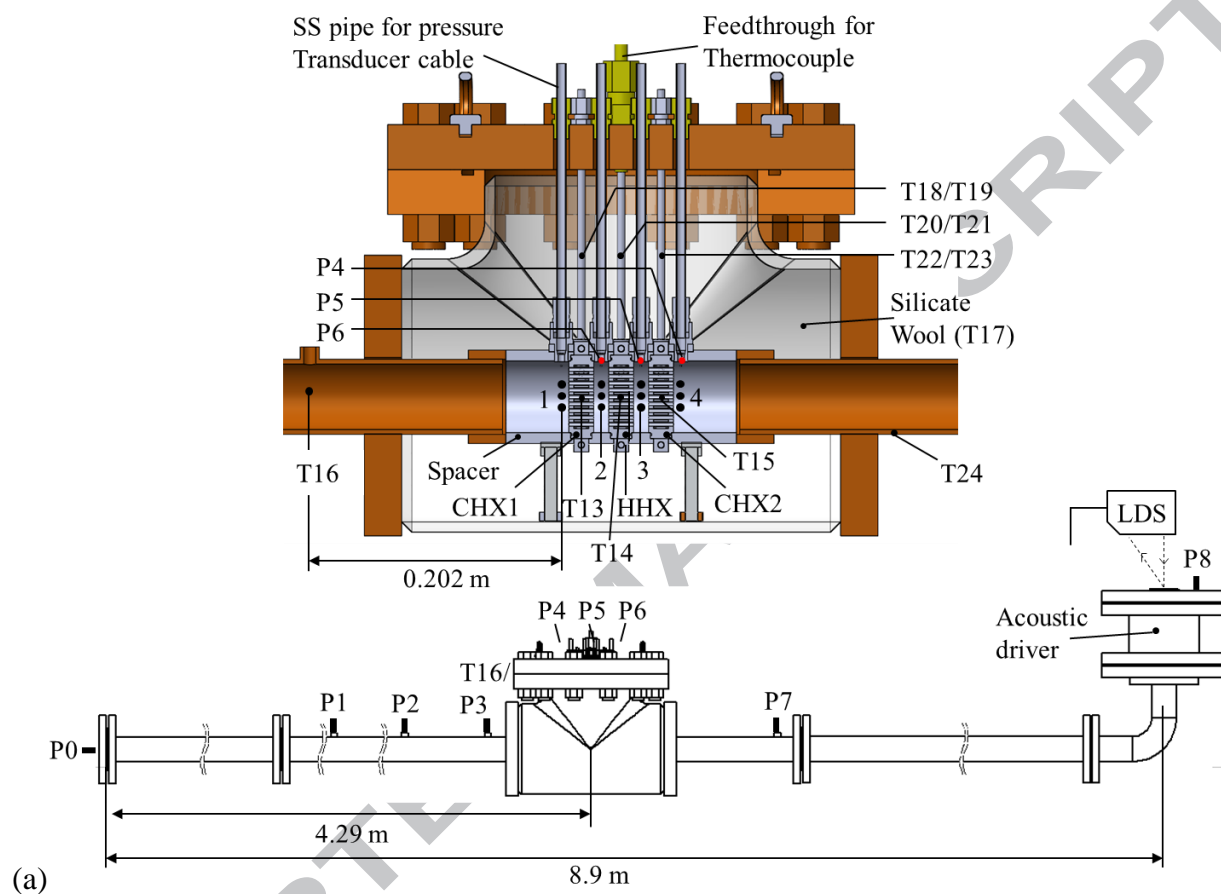
**Table 2:** Operating parameters and gas properties in the experiment and simulation

Operating parameter	Values
Mean pressure ( $P_m$ ), bar	5
Frequency of oscillation ( $f$ ), Hz	53.6
Drive ratio, %	$0.15 \leq DR \leq 1.29$
Temperature conditions:	
Hot heat exchanger (HHX)	30 - 150°C
Cold heat exchanger (CHX)	10°C
<b>Helium properties</b>	
Molar mass, kg/mol	0.04
Specific gas constant, J/kgK	2078.5
Specific heat capacity ( $c_p$ ), J/kg.K	5193
Speed of sound, m/s	1019.4

**Table 3:** Operating parameter based on experimental results ( $x = 4.29$  m) for T-HEX (flat)

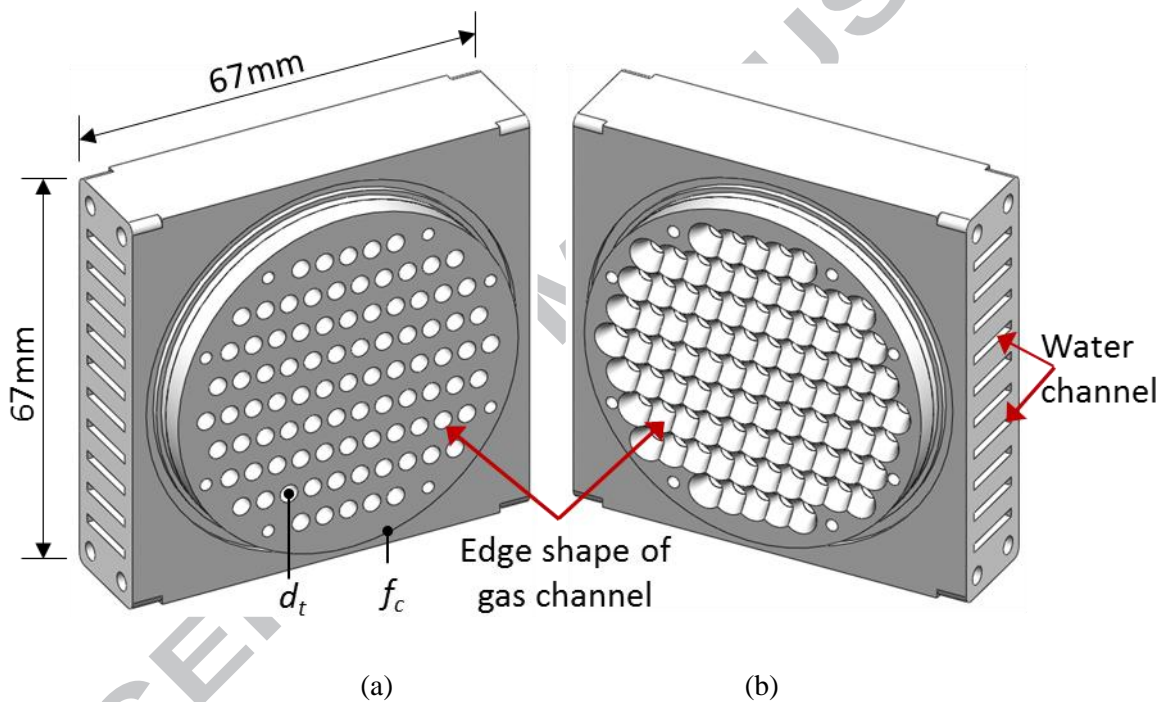
Drive Ratio (%)	Displacement Amplitude (mm)	Acoustic Reynolds Number (-)	Stokes Reynolds Number, $Re_s$ (-)
0.16	8.64	8,237	85.22
0.31	17.43	16,254	168.15
0.64	35.97	33,726	348.91
1.02	57.24	53,756	556.12
1.27	72.46	66,650	689.52

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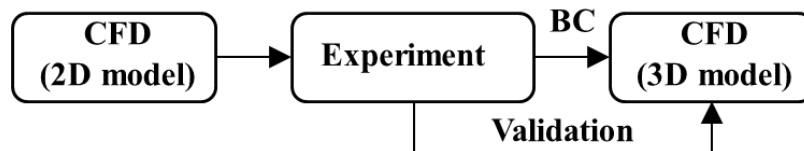


**Figure 1:** (a) CAD-image of the test section showing details of CHX1, HHX and CHX2 arrangement (top) and the drawing of experimental set-up (bottom). (b) Photograph of the test section location of the experimental set-up. LDS – Laser Display Sensor.

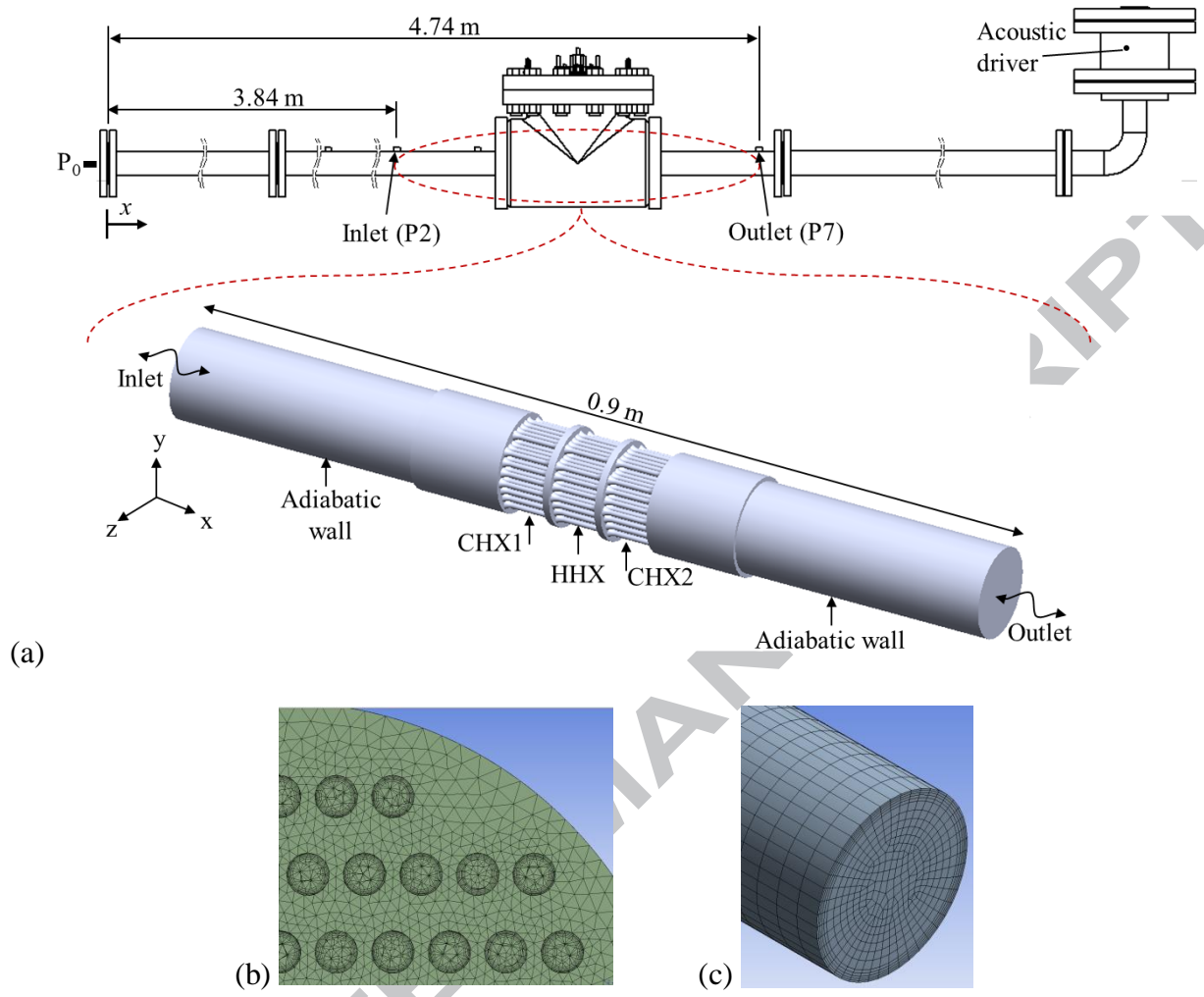
Locations  $x = 4.244, 4.276, 4.308$  and  $4.340$  m, are within the test section and they are used for data sampling during both the experiment and simulation. The oscillating variables at each location are identified with a number of the location as shown in Figure 1a (top), for example,  $x = 4.244$  m has temperature T-1 and pressure amplitude P-1.



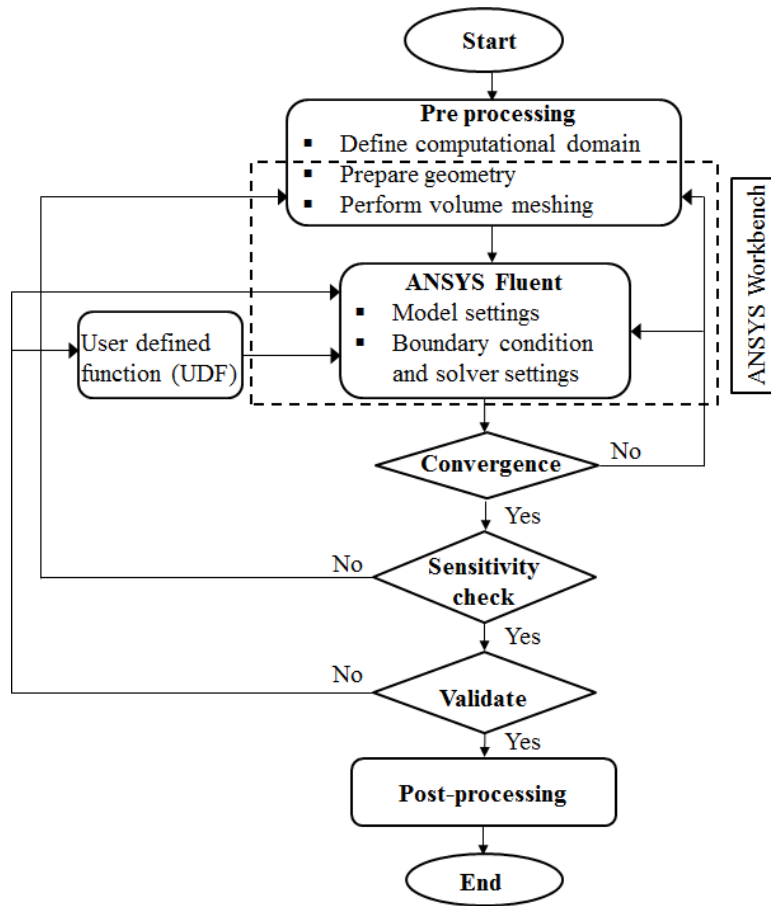
**Figure 2:** CAD-image of (a) T-HEX (flat) (b) T-HEX (ogive).



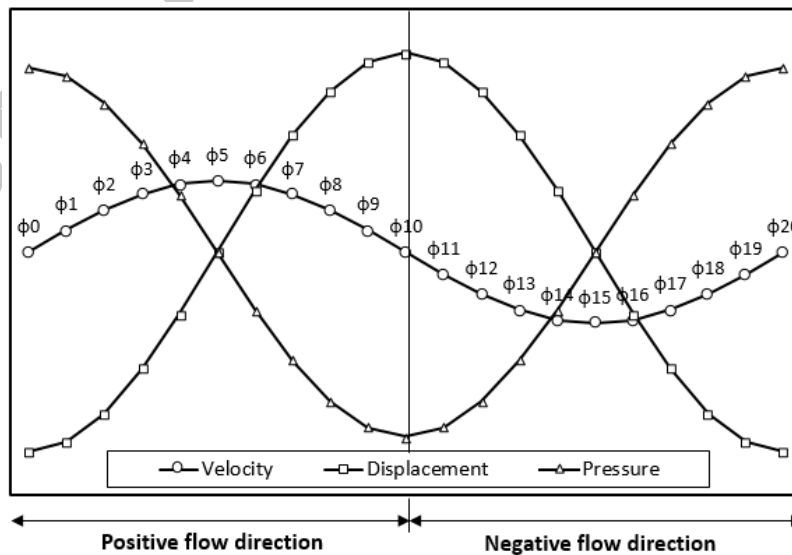
**Figure 3:** Approach for integrating the experiments with the Computational Fluid Dynamics (CFD) model. BC – Boundary Condition.



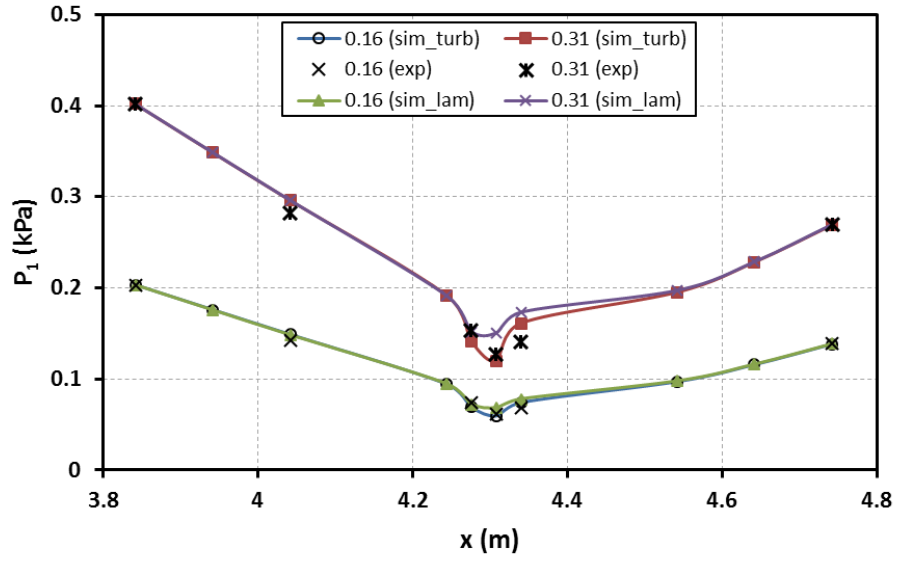
**Figure 4:** (a) Sketch of experimental set-up and computational domain (b) cut plane through HEX showing details of the gas channel (c) Inlet/Outlet of the meshed domain.



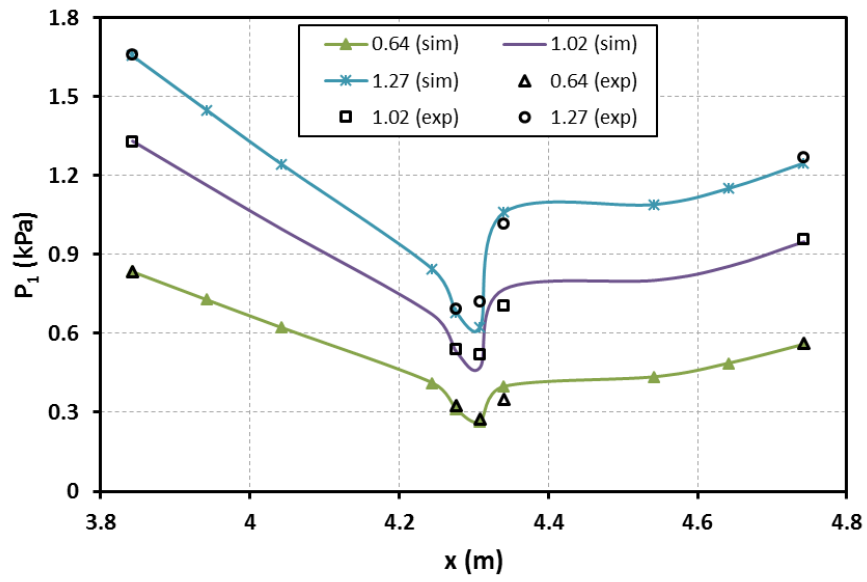
**Figure 5:** Flowchart of numerical solution procedure.



**Figure 6:** Relationship between the velocity, gas displacement and pressure amplitudes over the selected 20 phases in a flow cycle.

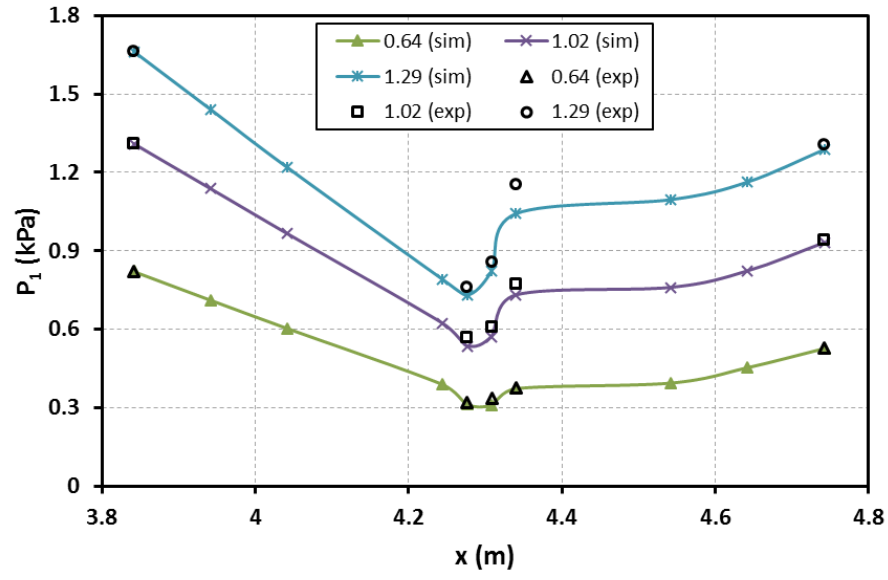
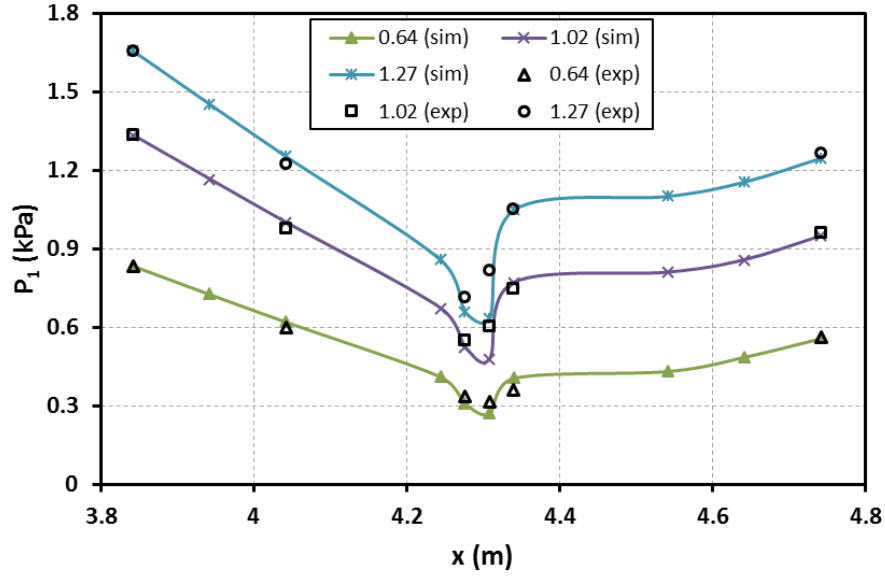


(a)

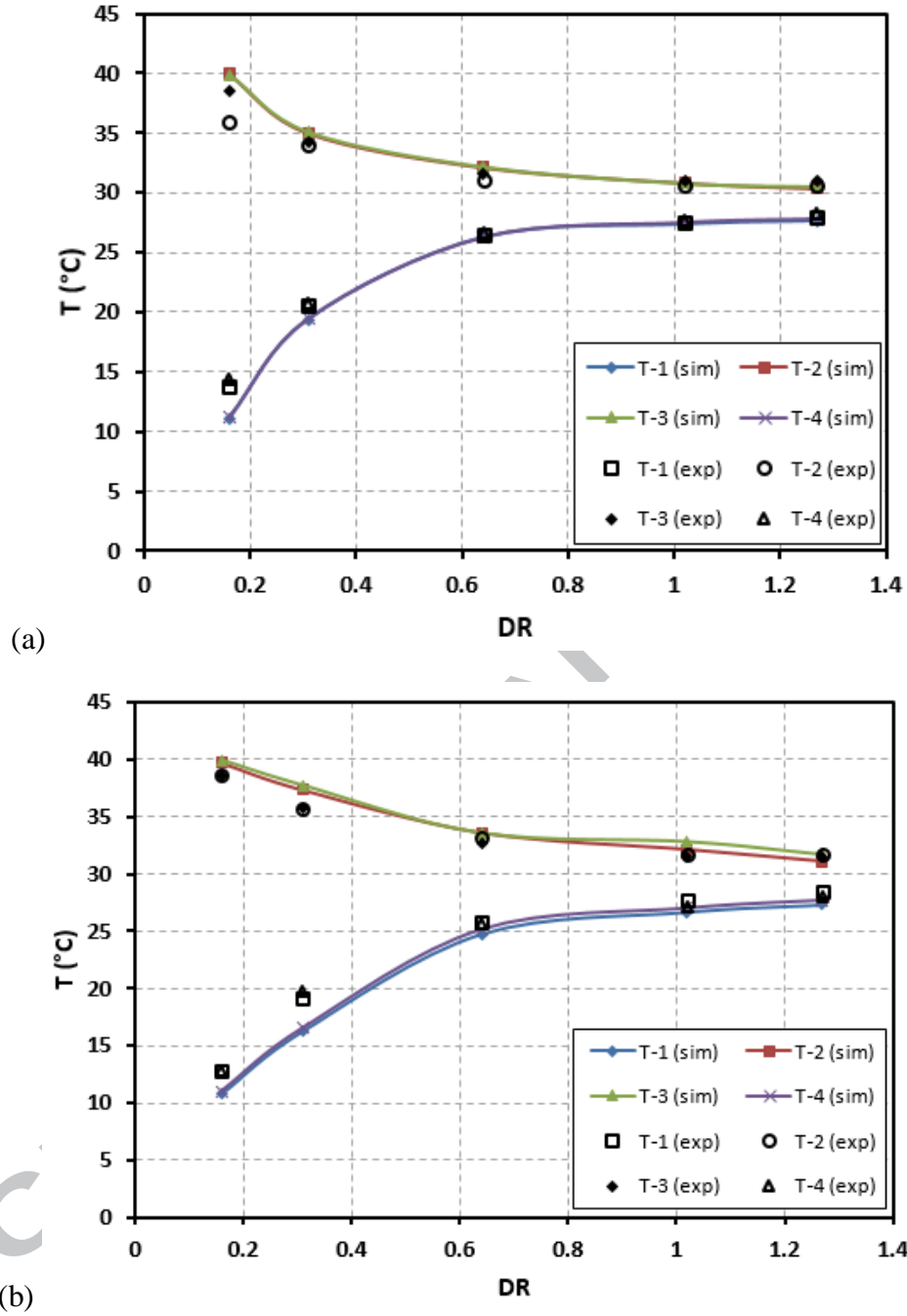


(b)

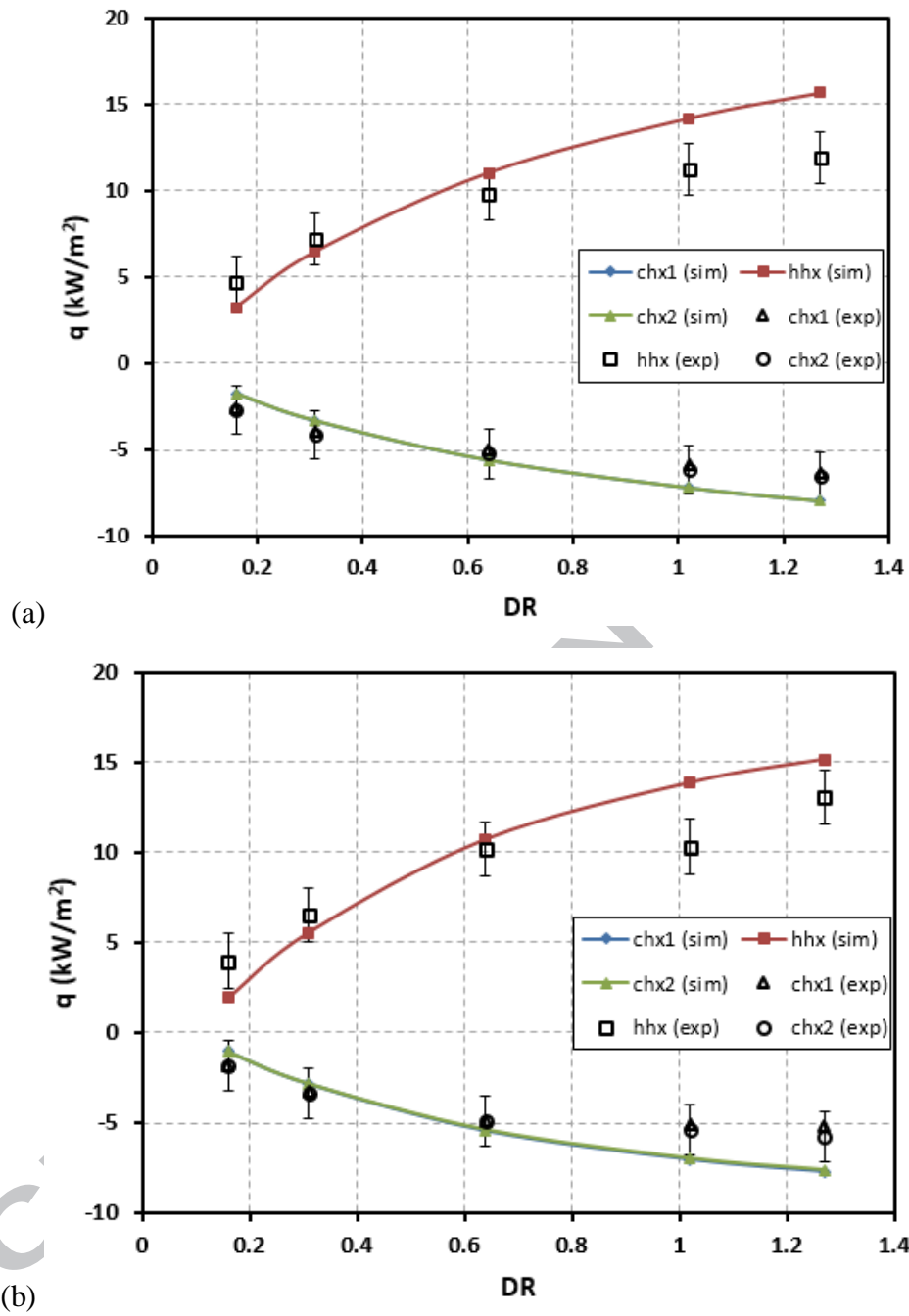




**Figure 7:** Comparison experimental (symbol) and numerical (solid line) pressure amplitudes (a) laminar and turbulence models (b) T-HEX(flat) at adiabatic (c) T-HEX(flat) with temperature (d) T-HEX(ogive) with temperature,  $T_h = 70^\circ\text{C}$ ,  $T_{c1,c2} = 10^\circ\text{C}$ .

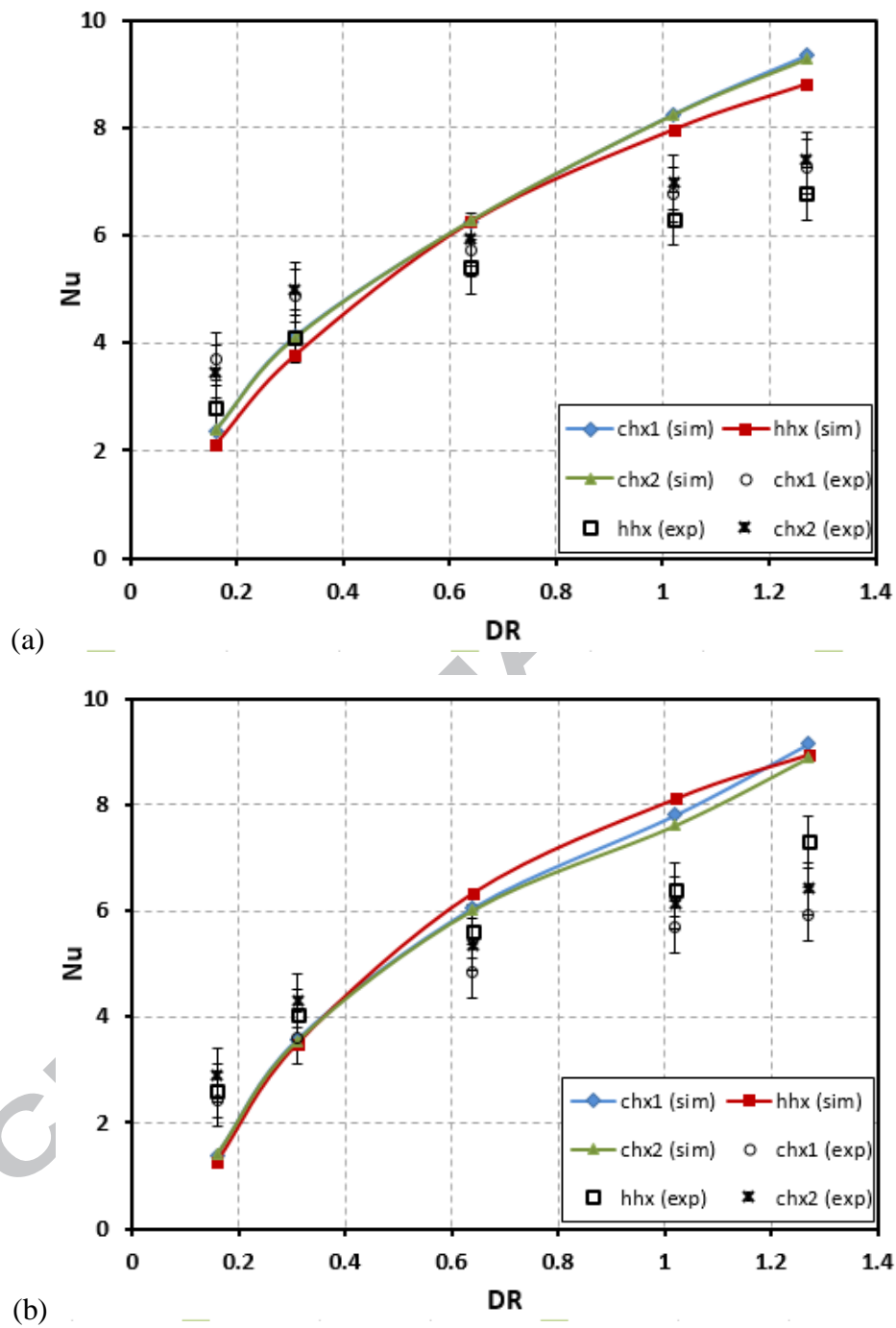


**Figure 8:** Comparison between experimental (symbols) and numerical (solid line) temperatures at locations  $x = 4.244, 4.276, 4.308$  and  $4.340$  m at  $T_h = 70^\circ\text{C}$ , (a) T-HEX (flat) (b) T-HEX (ogive).



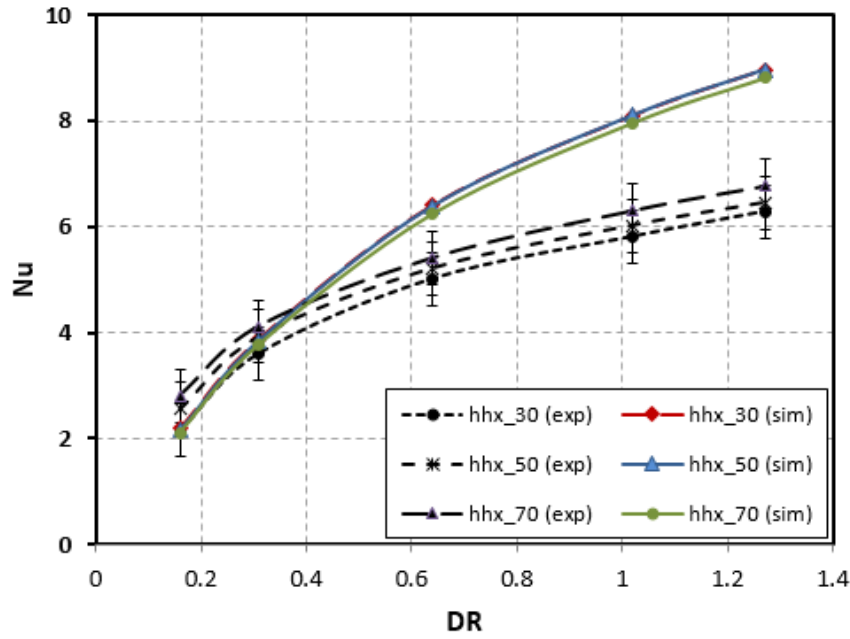
**Figure 9:** Comparison heat fluxes from experiment and simulation for (a) T-HEX (flat) (b) T-HEX (ogive).

*Nusselt number*

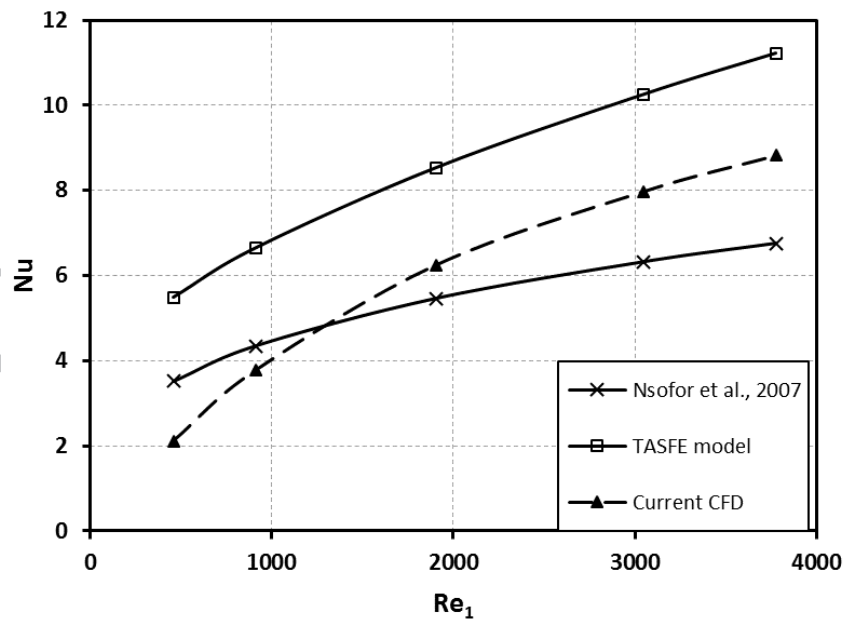


**Figure 10:** Nusselt number – experimental vs simulation results for (a) T-HEX (flat edge) (b) T-HEX (ogive).

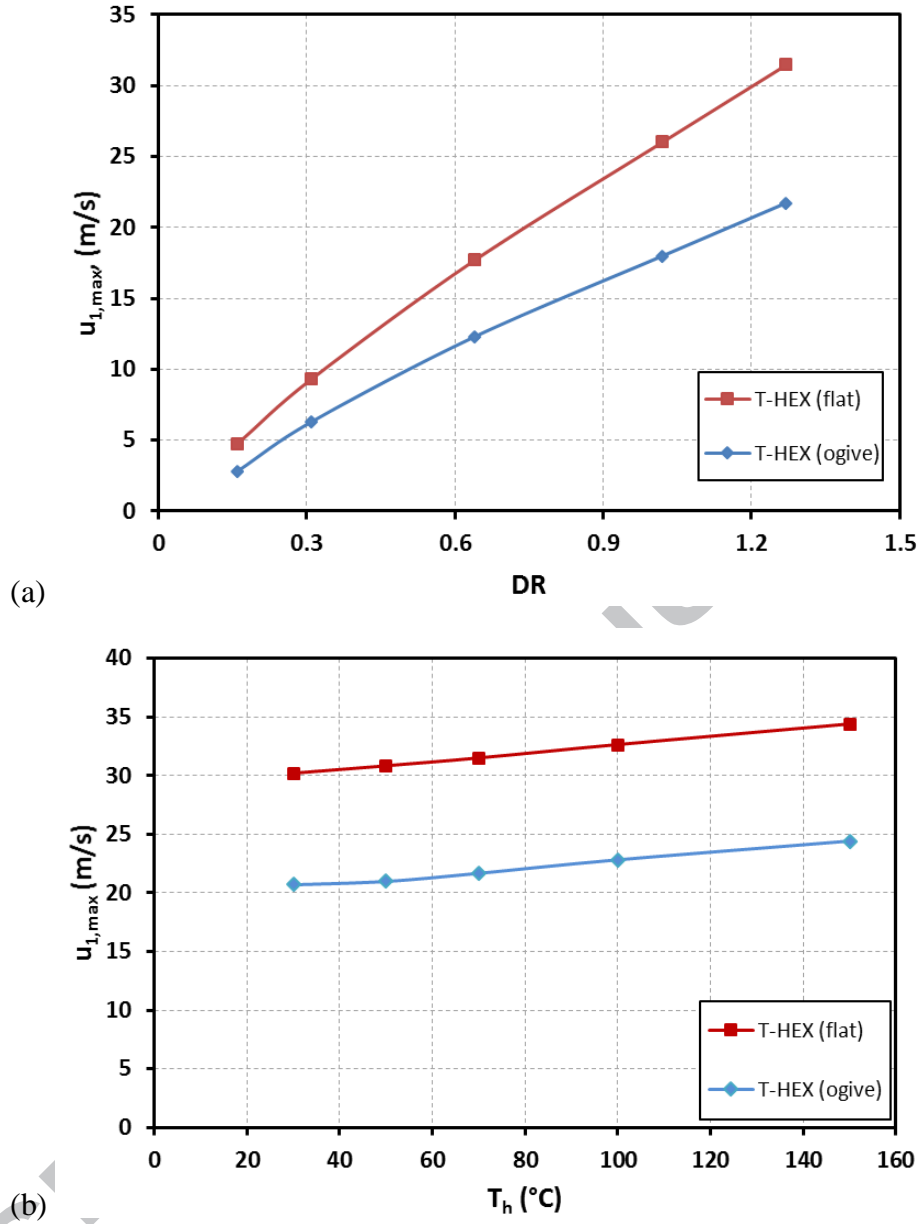
# Effect of temperature on $Nu$



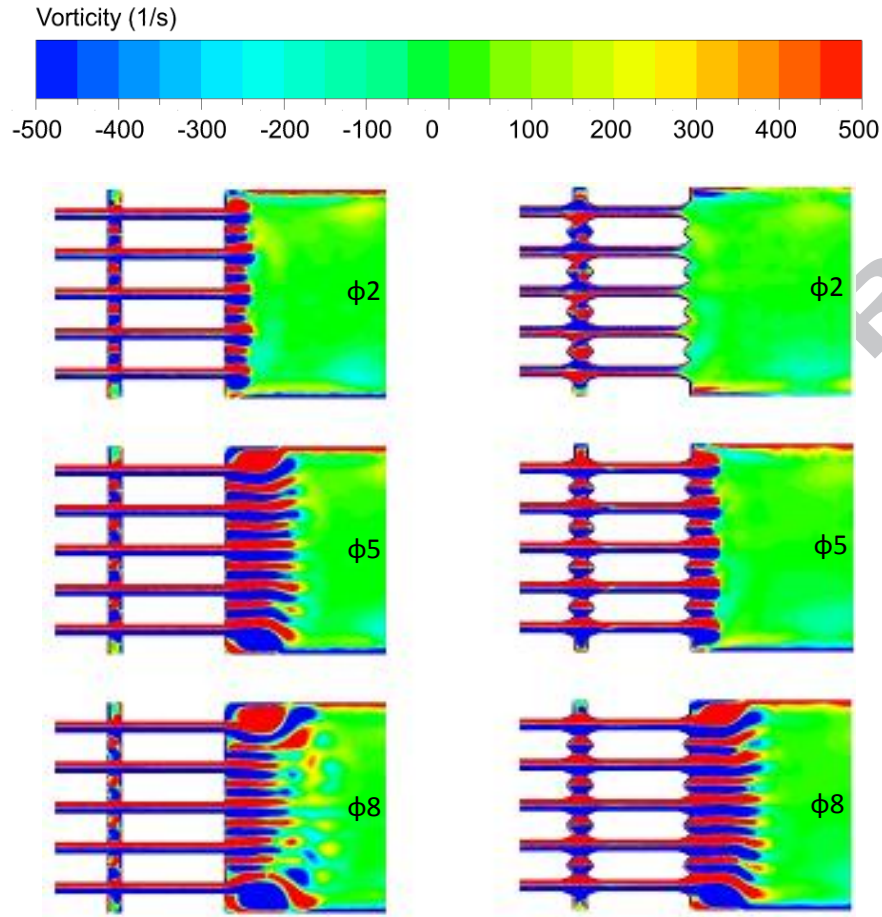
**Figure 11:** Effect of temperature on  $Nu$  at  $T_h = 30, 50,$  and  $70^\circ\text{C}$  for HHX (flat).



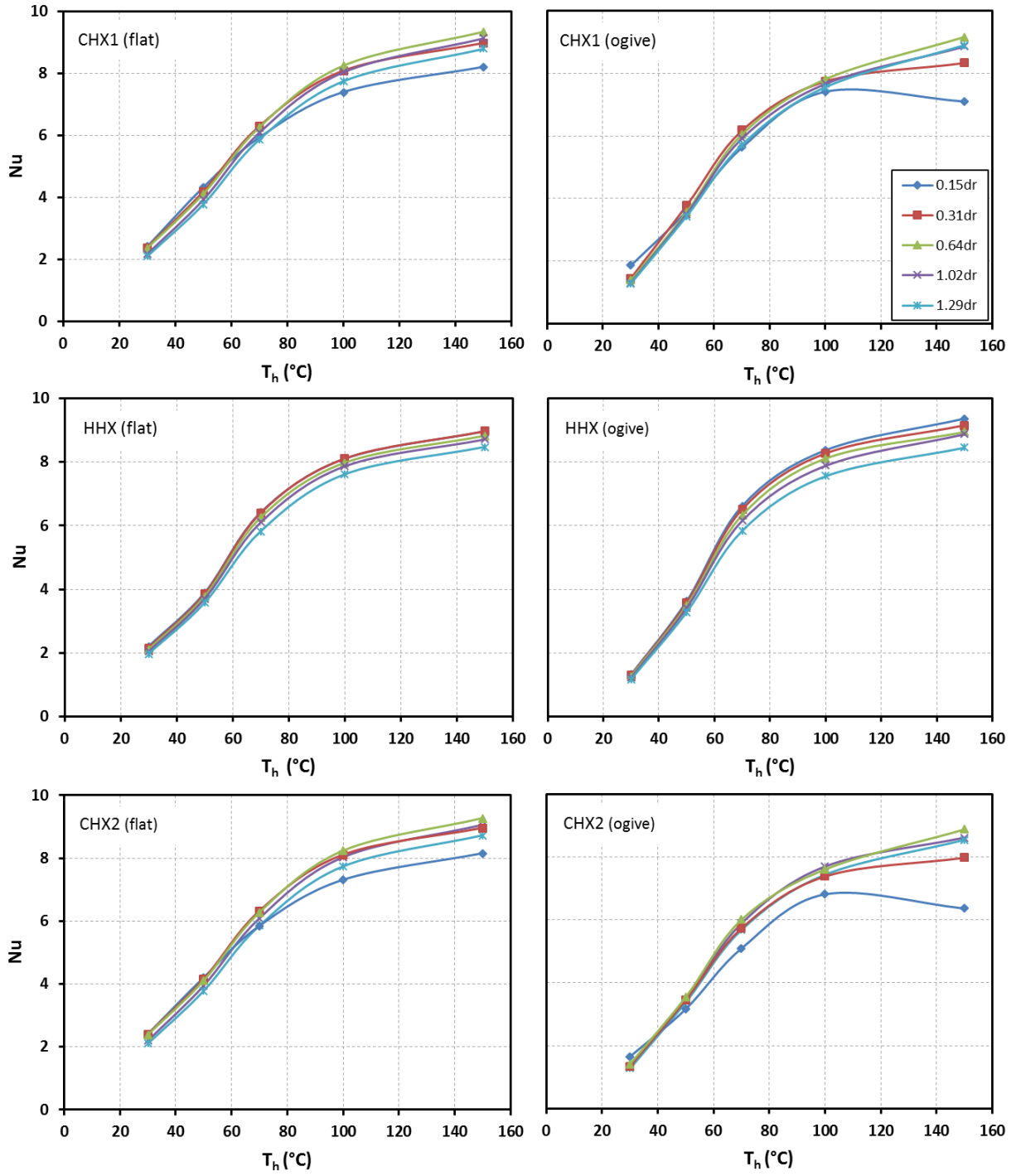
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**Figure 13:** Velocity amplitudes from the simulation result for T-HEX (flat) and T-HEX (ogive) (a) effect of  $DR$  at  $T_h = 70^\circ\text{C}$  ( $x = 4.32$ ) (b) Effect of temperature at  $DR = 1.29\%$ .

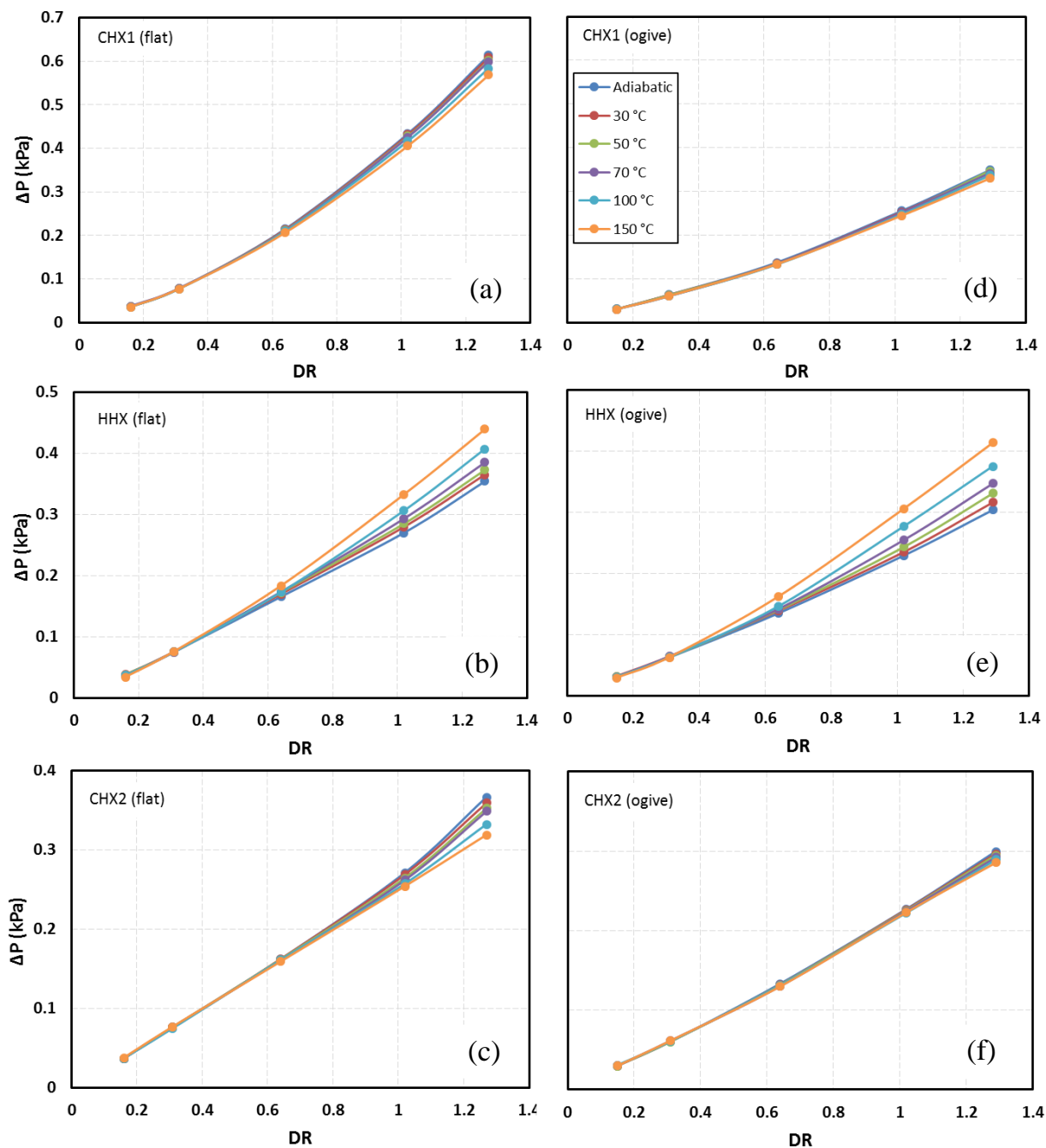


**Figure 14:** Vorticity contours – comparison between T-HEX (flat) and T-HEX (ogive) at  $T_h = 70^\circ\text{C}$ ,  $DR = 0.64\%$  (a)  $\phi 2$  (b)  $\phi 5$  (c)  $\phi 8$  (x-y plane (cf. Figure 1c)).



**Figure 15:** Effect of temperature on  $Nu$  for T-HEX (flat) and T-HEX (ogive) configuration.





**Figure 16:** Comparison between the predicted pressure drop across T-HEX (flat) and T-HEX (ogive).

### Highlights

- Heat transfer and pressure drop on Tube-Heat Exchangers in oscillatory flow tested
- Edge shape and symmetric arrangement of Heat Exchangers, and DR are considered
- Experimental and numerical Heat flux, Nu, and pressure drop are quantified
- Nu vs. ratio of maximum acoustic pressure to system mean pressure is established
- Ogive edge-shape minimises pressure drop with negligible effect on heat transfer